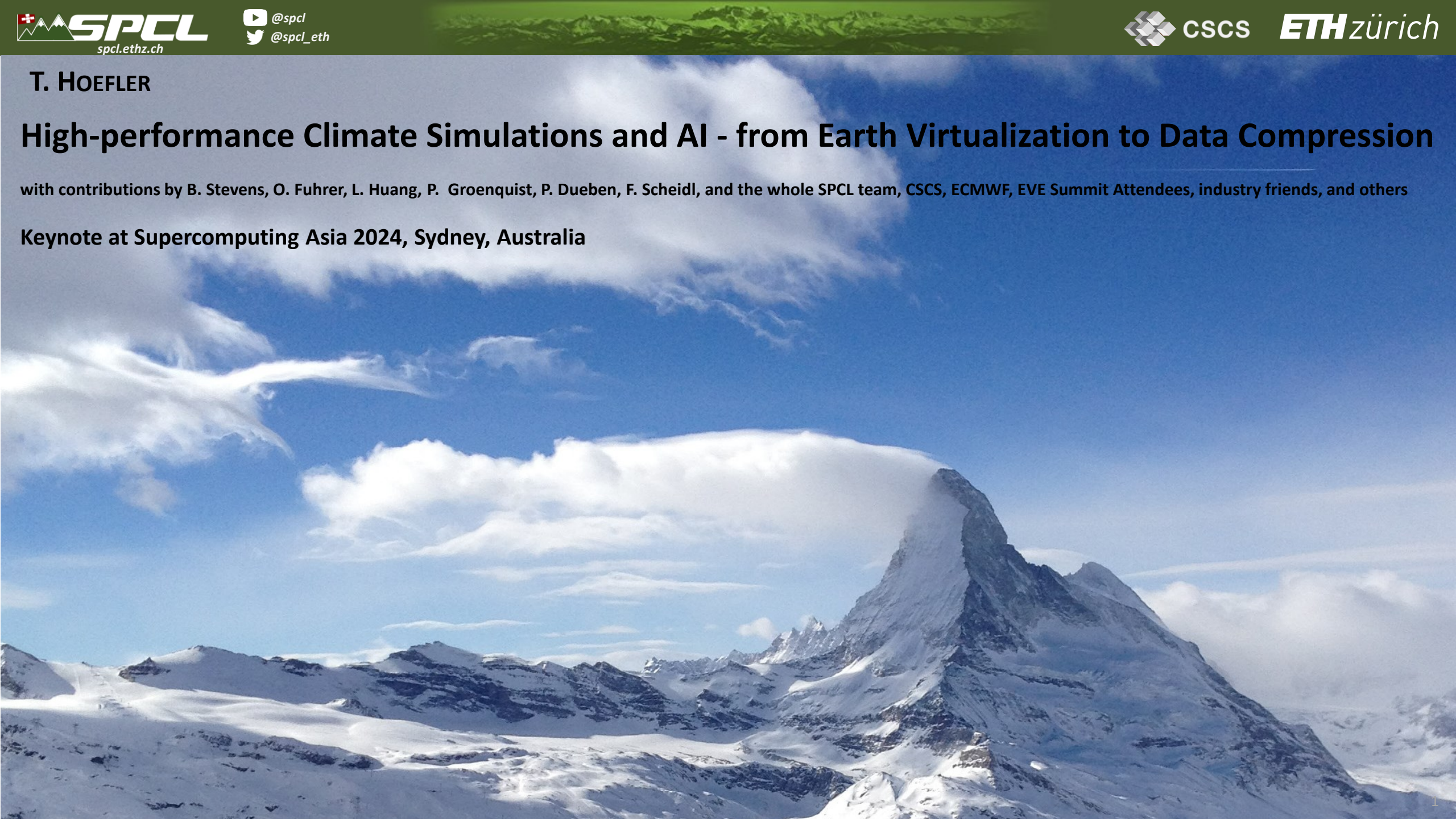



T. HOEFLER

High-performance Climate Simulations and AI - from Earth Virtualization to Data Compression

with contributions by B. Stevens, O. Fuhrer, L. Huang, P. Groenquist, P. Dueben, F. Scheidl, and the whole SPCL team, CSCS, ECMWF, EVE Summit Attendees, industry friends, and others

Keynote at Supercomputing Asia 2024, Sydney, Australia



 MENTOUR PILOT

ALWAYS HAVE
A BACKUP

LONDON, ENGLAND

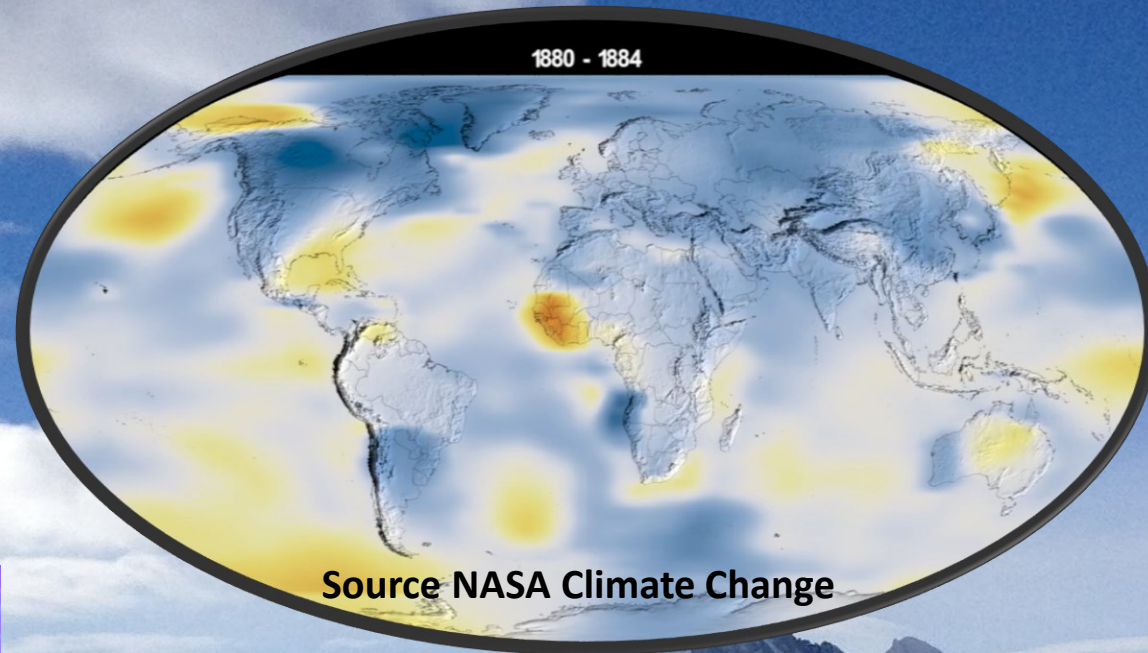
United Kingdom

T. HOEFLER

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Keynote at Supercomputing Asia 2024, Sydney, Australia



“Climate simulation is basically impossible today.”
“Predicting the average temperature is possible. However, the world doesn’t care about average. You care about your own region.” (Huang, Nov. 2023)

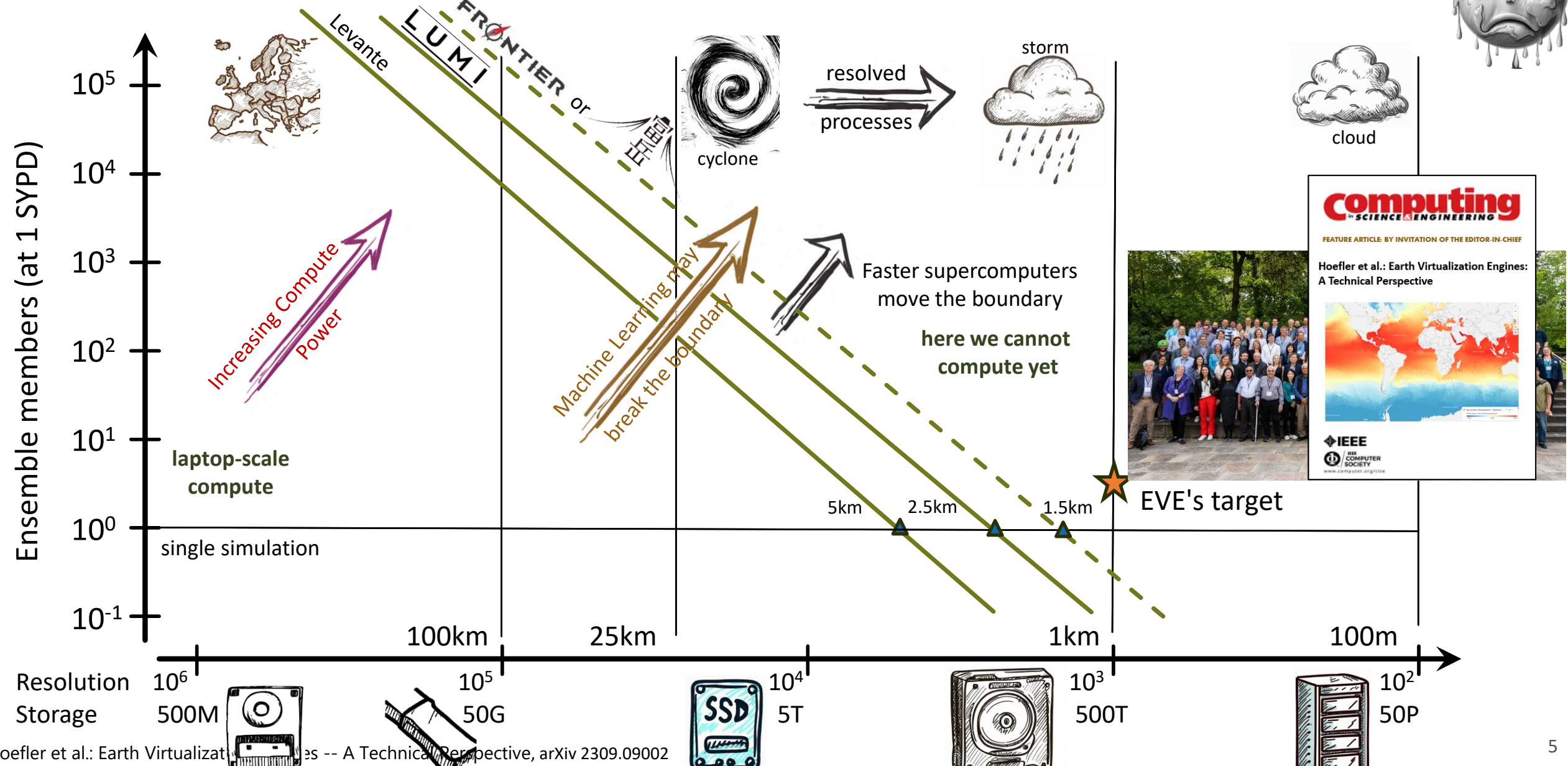
Earth Virtualization Engines Summit in Berlin

140 scientists from 93 institutions



Stevens et al.: “Earth Virtualization Engines (EVE)” (<https://essd.copernicus.org/preprints/essd-2023-376/>)

Climate prediction is extremely demanding ("impossible" – decades long)

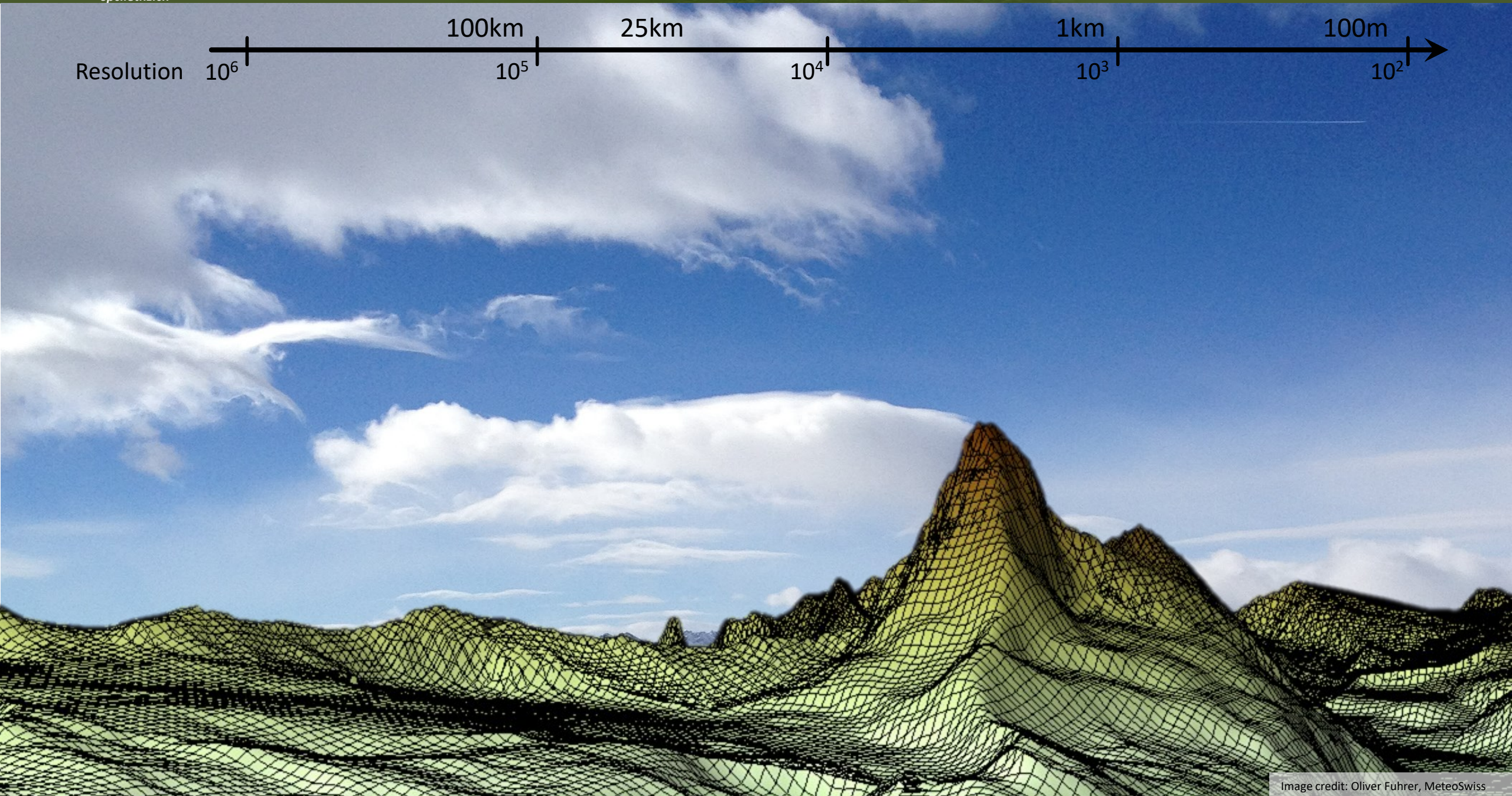


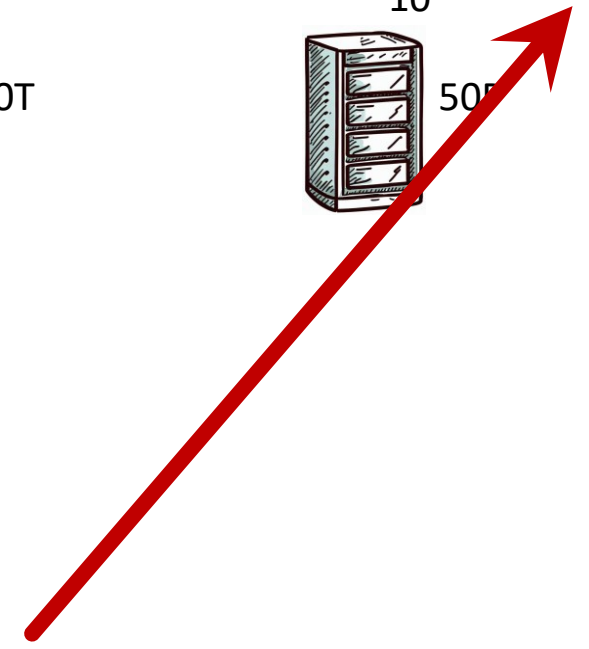
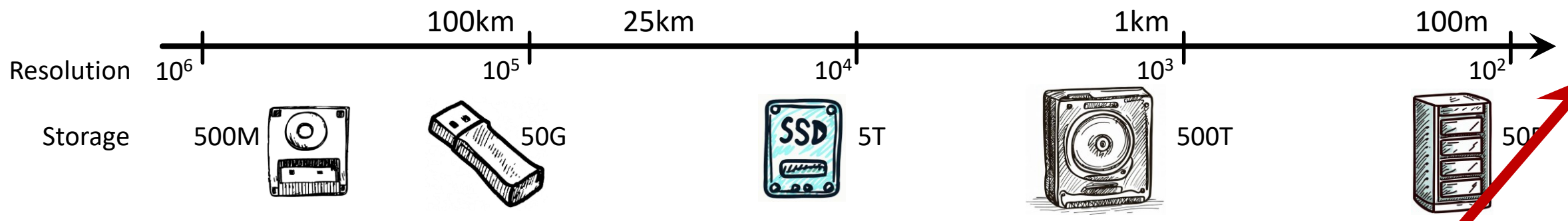
Earth Virtualization Engines Summit in Berlin

140 scientists from 93 institutions



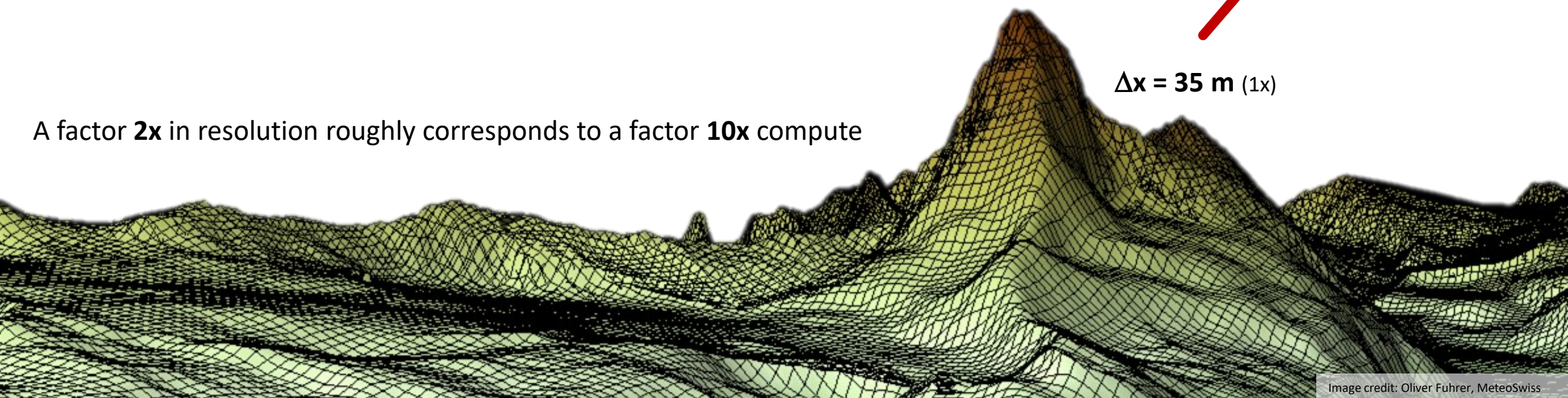
Icosahedral Nonhydrostatic Weather and Climate Model (ICON): >630k SLOC Fortran
30-year simulation at 1.23km (1 trajectory): 11 Zops, 13 days on Exascale (1% efficiency, 2.4 SYPD)
16k MPI processes, 3.25 GiB/s comm, 344 PiB of storage (7 vars, 15 min), 306 GiB/s average file I/O

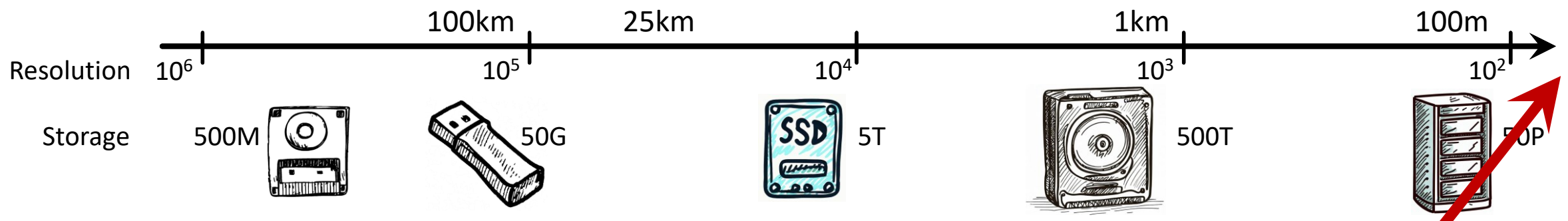




$\Delta x = 35 \text{ m (1x)}$

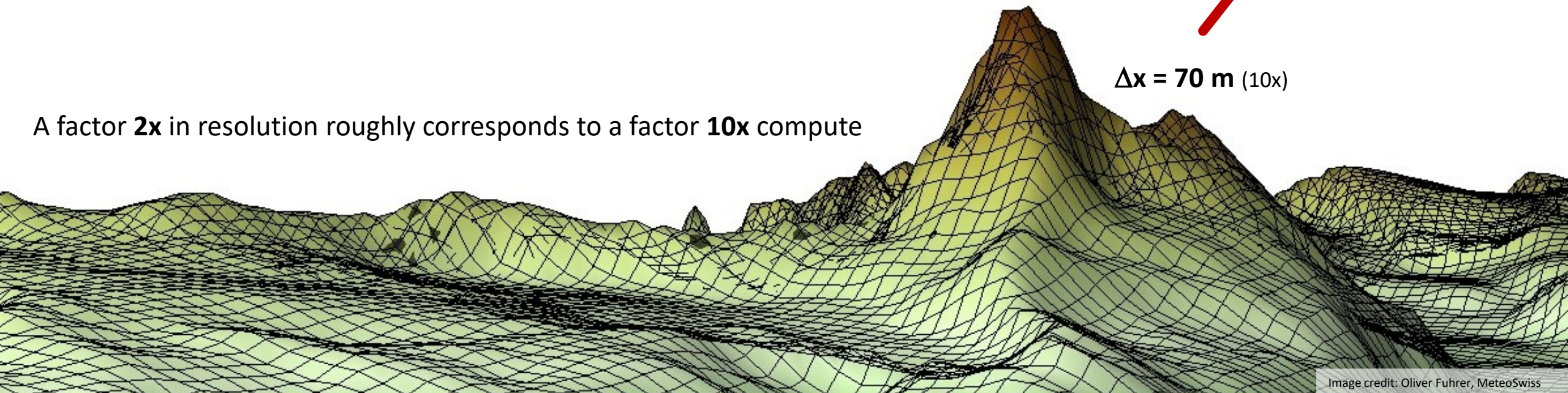
A factor **2x** in resolution roughly corresponds to a factor **10x** compute

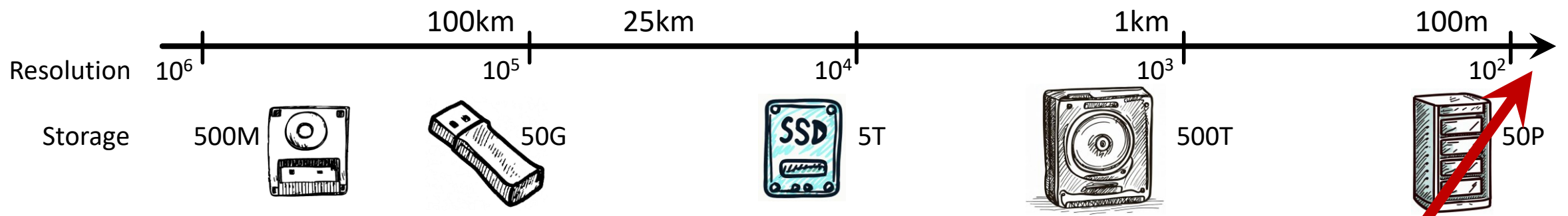




$\Delta x = 70 \text{ m (10x)}$

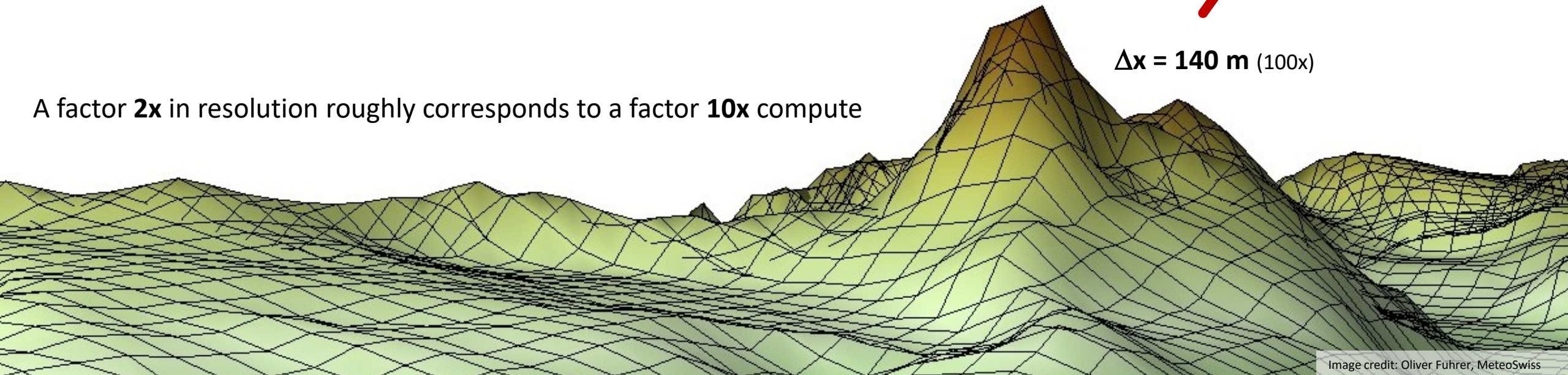
A factor **2x** in resolution roughly corresponds to a factor **10x** compute

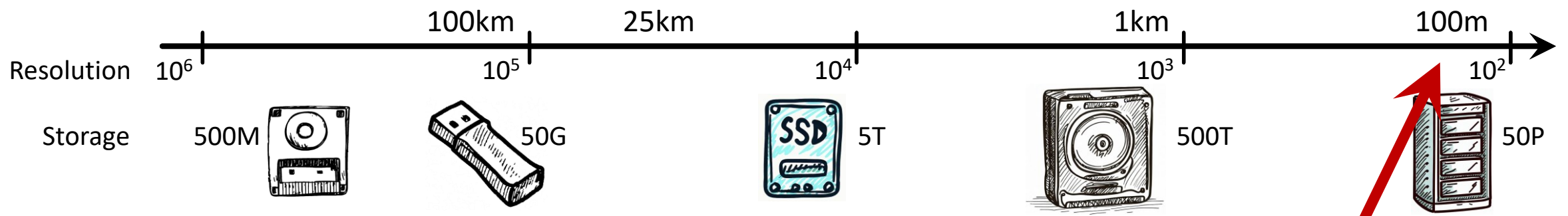




$\Delta x = 140 \text{ m}$ (100x)

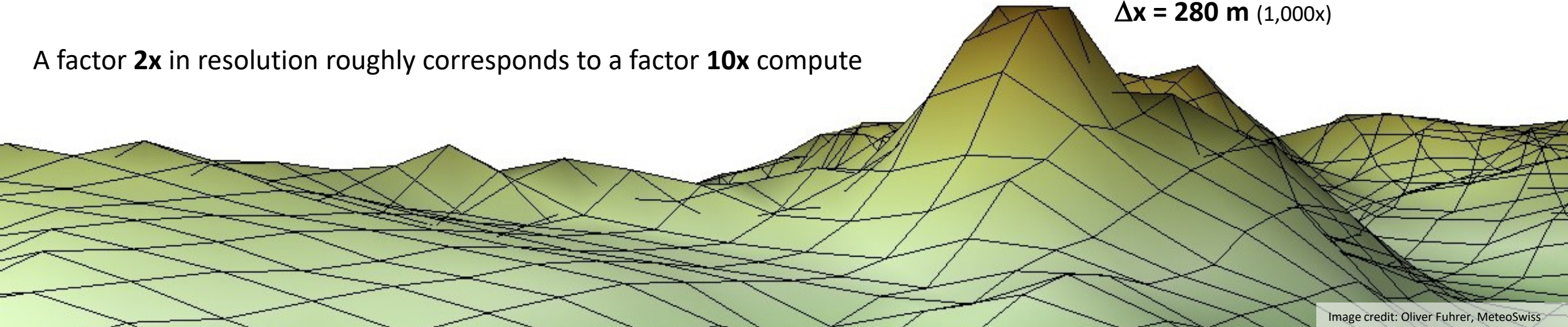
A factor **2x** in resolution roughly corresponds to a factor **10x** compute

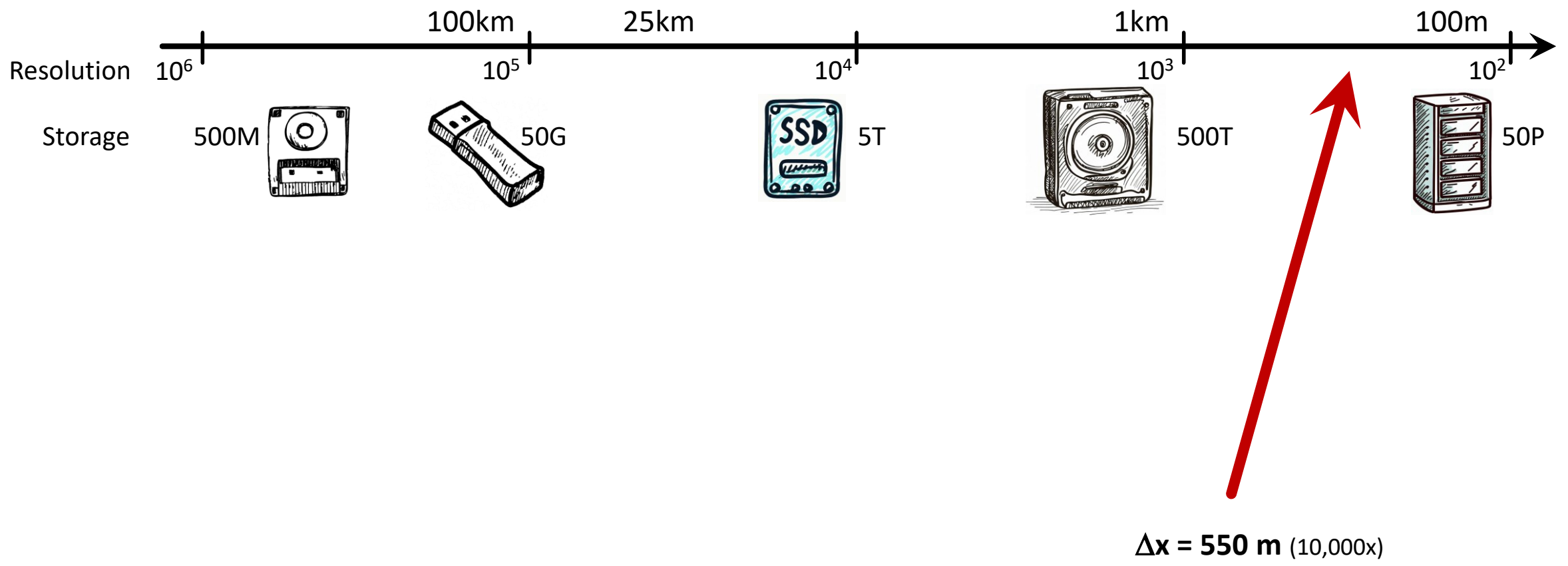




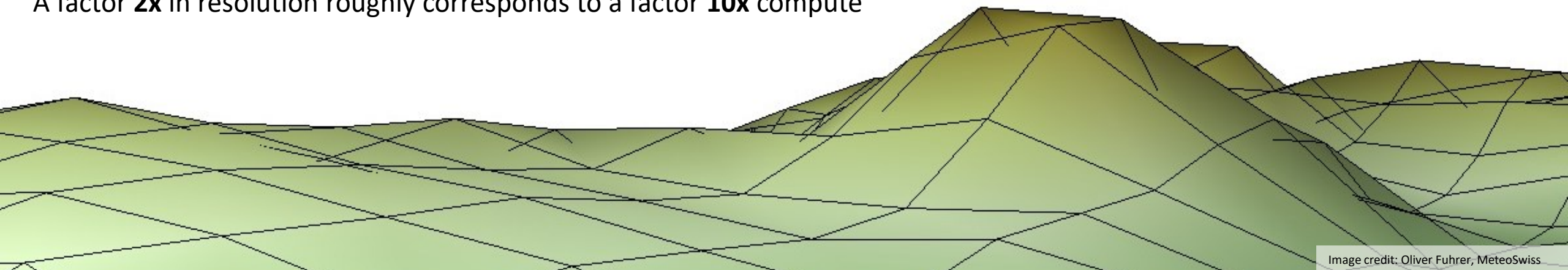
$\Delta x = 280 \text{ m}$ (1,000x)

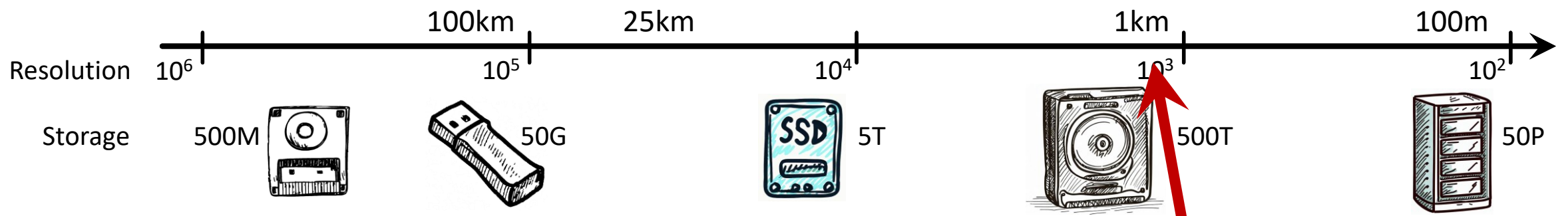
A factor **2x** in resolution roughly corresponds to a factor **10x** compute





A factor **2x** in resolution roughly corresponds to a factor **10x** compute

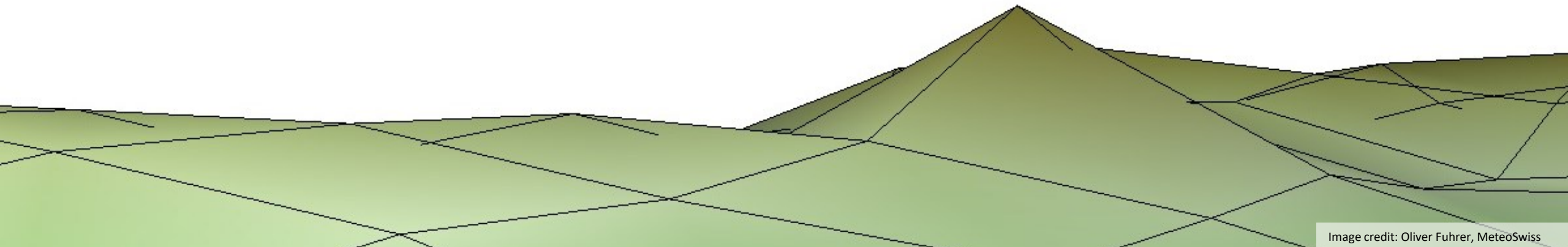


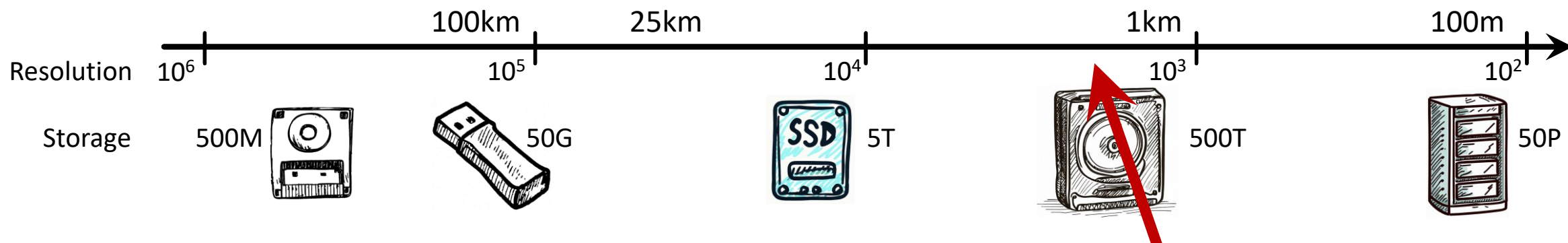


Operational weather model of MeteoSwiss today!

$\Delta x = 1100 \text{ m}$ (100,000x)

A factor **2x** in resolution roughly corresponds to a factor **10x** compute





Swiss to simulate weather using GPUs



SCIENTIFIC COMPUTING WORLD

2015

The Swiss Federal Office of Meteorology and Climatology (MeteoSwiss) has announced that it has taken delivery of the first GPU-accelerated supercomputer used to power the numerical weather forecasts.

Tech > Computing

CES 2019: Moore's Law is dead, says Nvidia's CEO

The long-held notion that the processing power of computers increases exponentially every couple of years has hit its limit, according to Jensen Huang.



Shara Tibken
Jan. 9, 2019 11:46 a.m. PT

3 min read

$\Delta x = 2200 \text{ m}$ (1,000,000x)

A factor **2x** in resolution roughly corresponds to a factor **10x** compute

Operational weather model of MeteoSwiss before 2016!

TECHNOLOGY

Nvidia CEO Says AI Can Overcome the Death of Moore's Law

By Tae Kim [Follow](#)

March 22, 2023, 1:35 pm EDT

A Changing High-P...

Bloomberg Subscribe

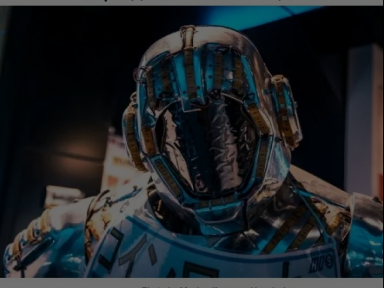
Technology | AI

ChatGPT to Fuel \$1.3 Trillion AI Market by 2032, New Report Says

- Bloomberg Intelligence expects generative AI market to soar
- Amazon, Microsoft, Google and Nvidia seen as biggest winners

By [Jake Rudnitsky](#)
 June 1, 2023 at 3:00 PM GMT+2
 Updated on June 1, 2023 at 5:50 PM GMT+2

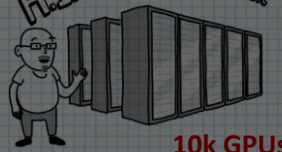
Chat GTP-4 Could Pass the Bar Exam
 How Our Technology Evolves FAST
 Source: <https://medium.com/>



AI chatbot's MBA exam
 business schools
 ChatGPT earned a solid grade and out...

Microsoft invests \$1 billion in OpenAI to pursue holy grail of artificial intelligence
 Building artificial general intelligence is OpenAI's ambitious goal
 By James Weston | Jul 22, 2019, 10:08am EDT

A.I. SUPERCOMPUTER
 10k GPUs



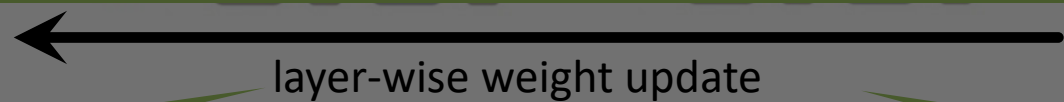
reddit



A robot may __ injure a

0.74	not	1.00
0.28	sometimes	0.00
0.07	always	0.00

Deep Learning Drives Future Computing Architectures!



Small datatypes
 (int + fp – 4, 8, 16 bits)
 Example: fp8 is 33x faster than fp64

Matrix and vector ops
 (tensor cores and vector units)
 Example: NVIDIA TCs: 8.3x over CUDA cores

(Structured) Sparsity
 (in tensor cores and vector units)
 Example: NVIDIA TCs: 2:4 sparsity

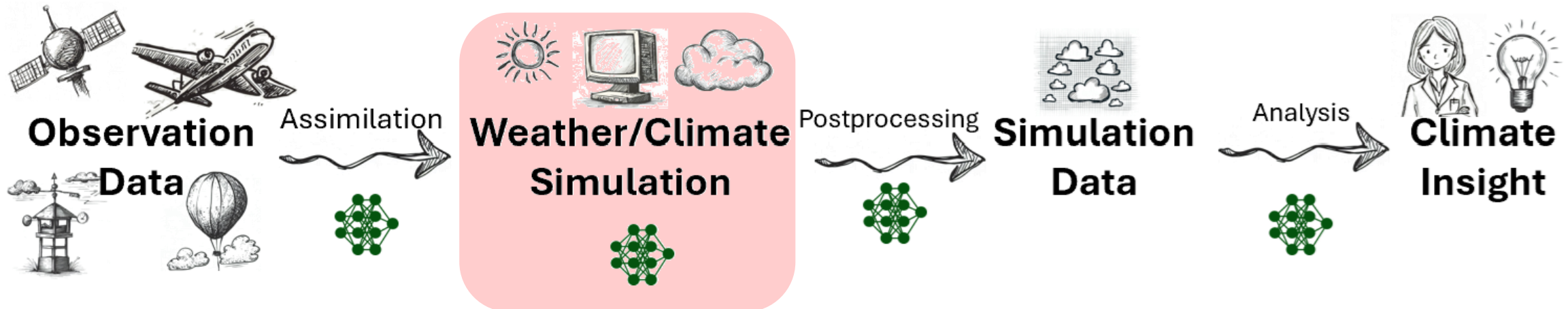
Embracing the future of accelerated computation

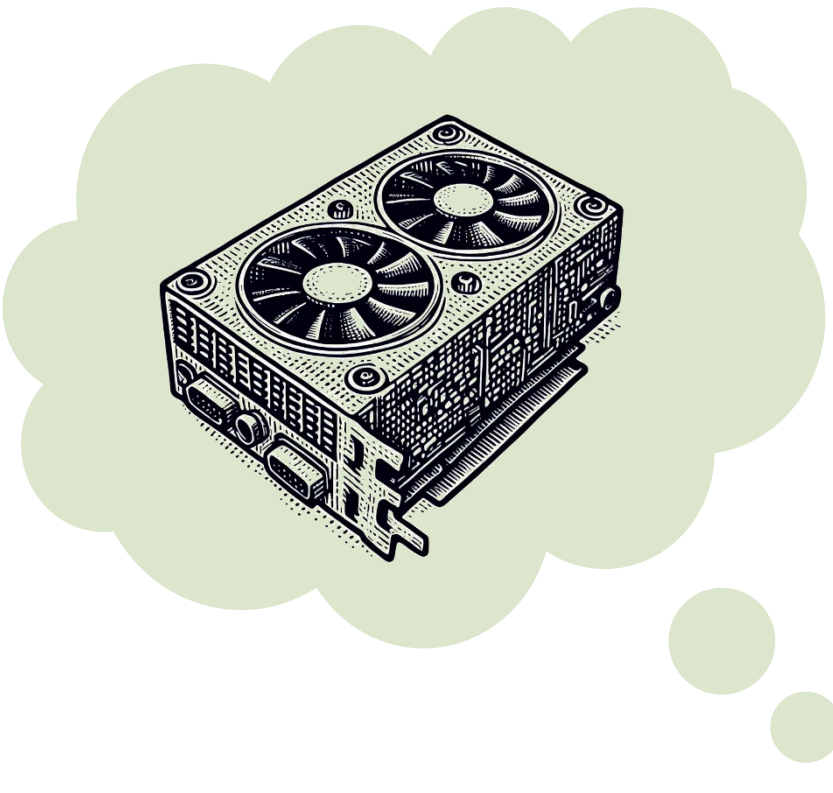
Accelerate Simulations on ML/AI Hardware

- Systems challenges:
 - Enable efficient GPU support
 - Optimize for data movement
- Algorithm challenges:
 - Make simulations look like low-precision matrix multiplication!

Use ML/AI Techniques (“ML inside/on top”)

- Use ML models to replace simulations completely
 - E.g., GraphCast, FourCastNet, PanGu, FuXi, ...
- Use ML to replace parts of the workflow
 - E.g., physics parametrization in simulations, data post processing, analyses, ...





```

!$ACC DATA &
!$ACC PRESENT(density1,energy1) &
!$ACC PRESENT(vol_flux_x,vol_flux_y,volume,mass_flux_x,mass_flux_y,vertexdx,vertexdy) &
!$ACC PRESENT(pre_vol,post_vol,ener_flux)

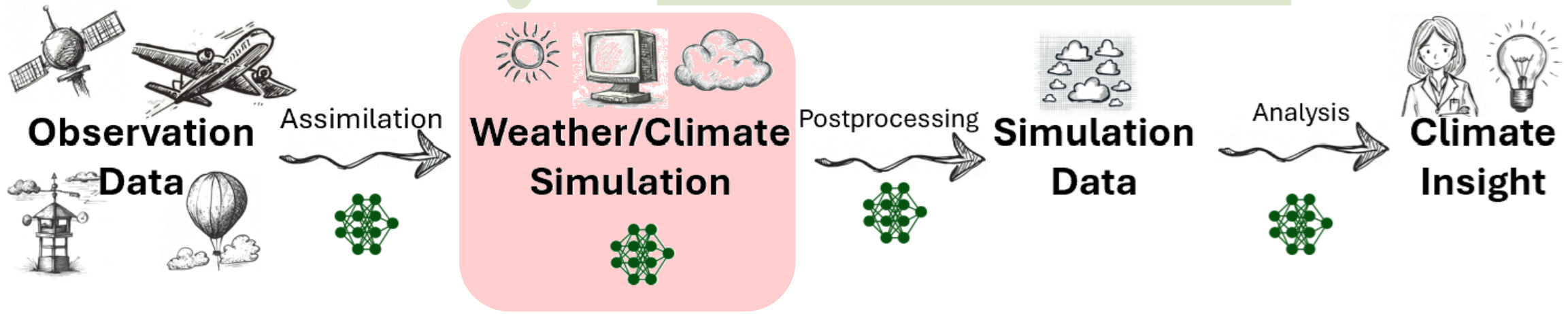
!$ACC KERNELS

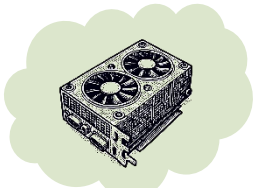
IF(dir.EQ.g_xdir) THEN

IF(sweep_number.EQ.1)THEN

!$ACC LOOP INDEPENDENT
DO k=y_min-2,y_max+2
!$ACC LOOP INDEPENDENT
DO j=x_min-2,x_max+2
pre_vol(j,k)=volume(j,k)+(vol_flux_x(j+1,k )-vol_flux_x(j,k)+vol_flux_y(j ,k+1)-vol_flux_y(j,k))
post_vol(j,k)=pre_vol(j,k)-(vol_flux_x(j+1,k )-vol_flux_x(j,k))
ENDDO
ENDDO
ELSE
!$ACC LOOP INDEPENDENT
DO k=y_min-2,y_max+2
!$ACC LOOP INDEPENDENT
DO j=x_min-2,x_max+2
pre_vol(j,k)=volume(j,k)+vol_flux_x(j+1,k)-vol_flux_x(j,k)
post_vol(j,k)=volume(j,k)
ENDDO
ENDDO

ENDIF
  
```





!\$ACC DATA &

```

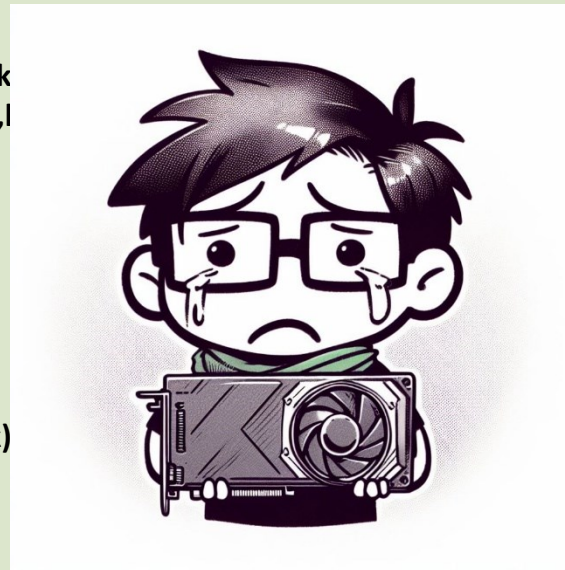
!$ACC COPY(chunk%tiles(1)%field%density0) &
!$ACC COPY(chunk%tiles(1)%field%density1) &
!$ACC COPY(chunk%tiles(1)%field%energy0) &
!$ACC COPY(chunk%tiles(1)%field%energy1) &
!$ACC COPY(chunk%tiles(1)%field%pressure) &
!$ACC COPY(chunk%tiles(1)%field%soundspeed) &
!$ACC COPY(chunk%tiles(1)%field%viscosity) &
!$ACC COPY(chunk%tiles(1)%field%xvel0) &
!$ACC COPY(chunk%tiles(1)%field%yvel0) &
!$ACC COPY(chunk%tiles(1)%field%xvel1) &
!$ACC COPY(chunk%tiles(1)%field%yvel1) &
!$ACC COPY(chunk%tiles(1)%field%vol_flux_x) &
!$ACC COPY(chunk%tiles(1)%field%vol_flux_y) &
!$ACC COPY(chunk%tiles(1)%field%mass_flux_x)&
!$ACC COPY(chunk%tiles(1)%field%mass_flux_y)&
!$ACC COPY(chunk%tiles(1)%field%volume) &
!$ACC COPY(chunk%tiles(1)%field%work_array1)&
!$ACC COPY(chunk%tiles(1)%field%work_array2)&
!$ACC COPY(chunk%tiles(1)%field%work_array3)&
!$ACC COPY(chunk%tiles(1)%field%work_array4)&
!$ACC COPY(chunk%tiles(1)%field%work_array5)&
!$ACC COPY(chunk%tiles(1)%field%work_array6)&
!$ACC COPY(chunk%tiles(1)%field%work_array7)&
!$ACC COPY(chunk%tiles(1)%field%cellx) &
!$ACC COPY(chunk%tiles(1)%field%celly) &
!$ACC COPY(chunk%tiles(1)%field%celldx) &
!$ACC COPY(chunk%tiles(1)%field%celldy) &
!$ACC COPY(chunk%tiles(1)%field%vertexx) &
!$ACC COPY(chunk%tiles(1)%field%vertexdx) &
!$ACC COPY(chunk%tiles(1)%field%vertexy) &
!$ACC COPY(chunk%tiles(1)%field%vertexdy) &
!$ACC COPY(chunk%tiles(1)%field%xarea) &
!$ACC COPY(chunk%tiles(1)%field%yarea) &
!$ACC COPY(chunk%left_snd_buffer) &
!$ACC COPY(chunk%left_rcv_buffer) &
!$ACC COPY(chunk%right_snd_buffer) &
!$ACC COPY(chunk%right_rcv_buffer) &
!$ACC COPY(chunk%bottom_snd_buffer) &
!$ACC COPY(chunk%bottom_rcv_buffer) &
!$ACC COPY(chunk%top_snd_buffer) &
!$ACC COPY(chunk%top_rcv_buffer)
  
```

Sloccount *f90: 6,440
 ,mass_flux_x,mass_flux_y,vertexdx,vertexdy) &

!\$ACC: 833 (13%)

1,k
 r,1,

l,k)



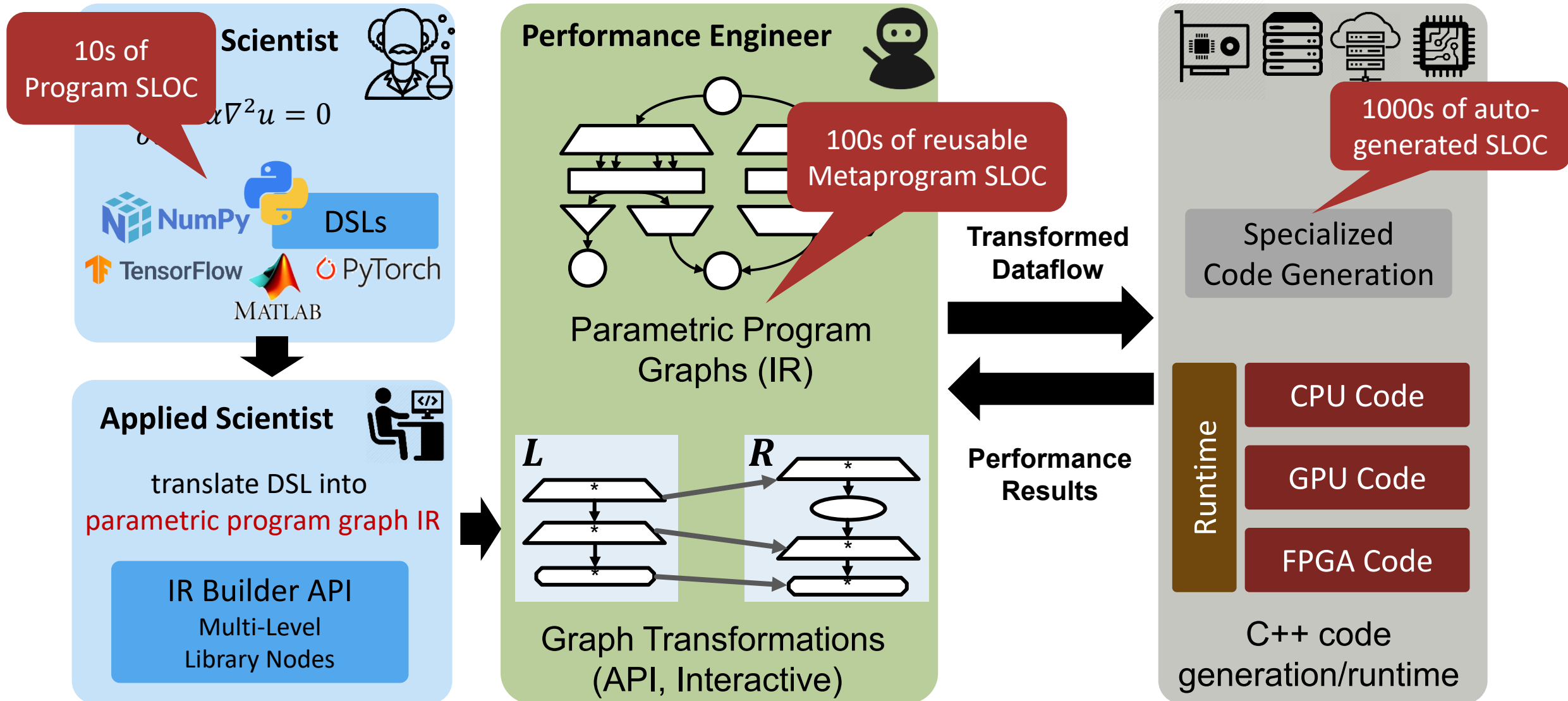
Heitlager et al.: A Practical Model for Measuring Maintainability

source code properties

	volume	complexity per unit	duplication	unit size	unit testing
analysability	X		X	X	X
changeability		X	X		
stability					X
testability		X		X	X

ISO 9126 maintainability

Performance Metaprogramming for Optimization and Performance Portability



The Pace Project

- NOOA's FV3 reimaged in Python

- Goal: Atmospheric model that can run at scale on modern supercomputers
- No FORTRAN involved – move to 21st century programming + devops + package management (with similar syntax!)

- Full dynamical core: 12,450 Python LoC across 36 modules

vs. 29,458 in the baseline implementation

 <https://github.com/ai2cm/pace>

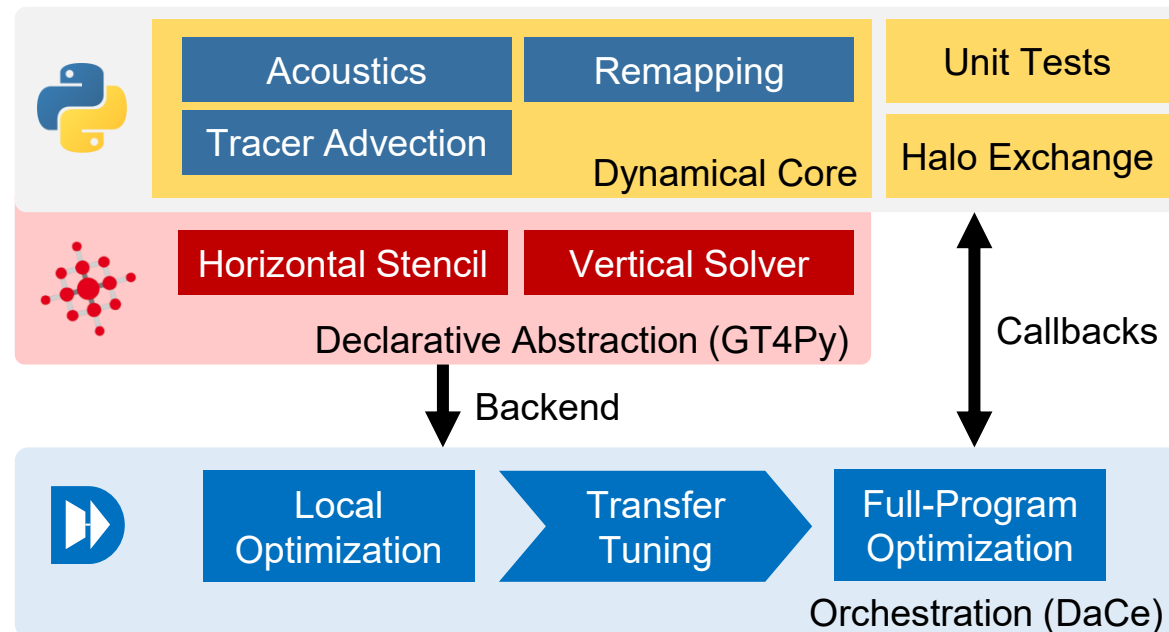
```

Usage: python -m pace.driver.run [OPTIONS] CONFIG_PATH

Run the driver.

CONFIG_PATH is the path to a DriverConfig yaml file.

Options:
...
  
```



Building around GridTools/Gt4Py



Pace in DaCe for **Performance Metaprogramming** – 12k SLOC Python

AI-based Transfer Tuning to the Rescue!



T. HOEFLER

AI-Driven Performance Metaprogramming

with contributions by the whole SPCL deep learning team (T. Ben-Nun, S. Jakobovits, L. Truemper, A. Calotoiu, and many others) and collaborators (C. Cummins and others)

Keynote talk at the AI for Developers Workshop @ Supercomputing 2023, Denver, CO, 2023





Evaluated Systems

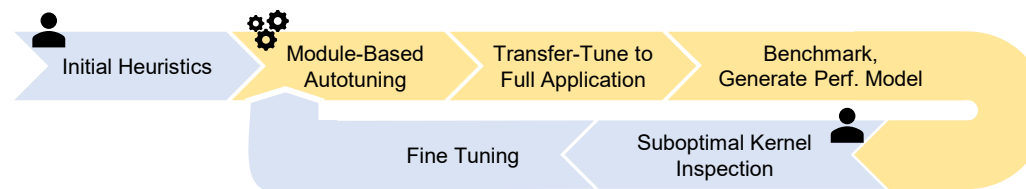
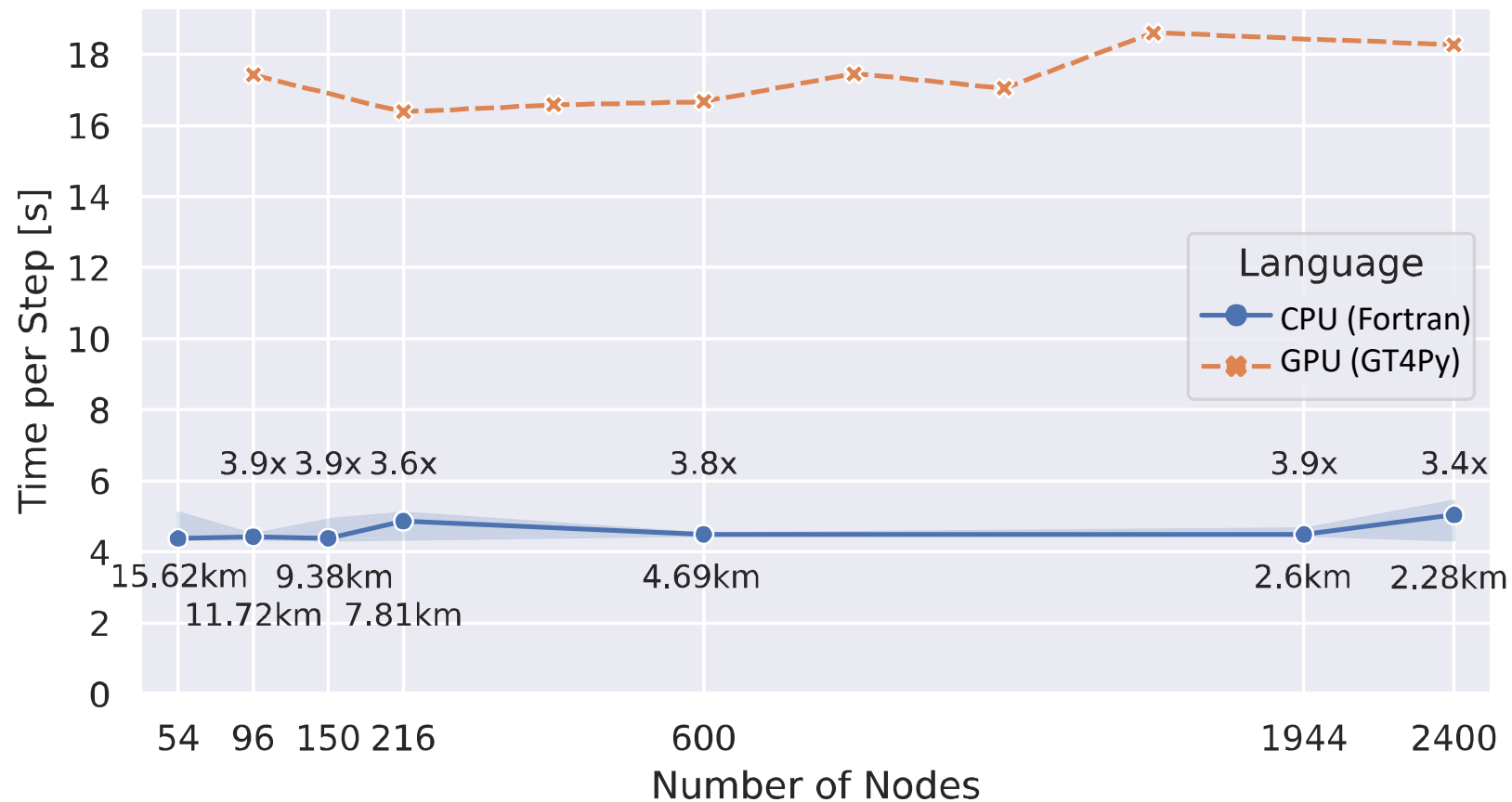


Photo courtesy of the [Swiss National Supercomputing Centre](https://www.sns.ch/)

Piz Daint:

- GPU: 1 x NVIDIA Tesla P100 / Node
- CPU: Intel Xeon E5-2690 v3 (12 cores)

Per-node domain size: 192x192x80



Simulation throughput of **0.12 SYPD** at 2.6 km grid spacing

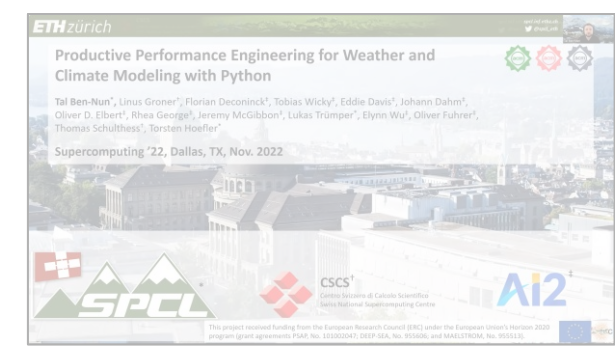

<https://github.com/ai2cm/pace>
<https://github.com/GridTools/gt4py>
<https://github.com/spcl/dace>



That's all nice but do we really want to rewrite all codes?

6	10	4	3.92 – 8.48x	0
weeks of work	optimization revisions	performance engineers	speedup vs. production FORTRAN	model changes

 youtube.com/@spcl



Another real production code ... ECMWF's CLOUDSC

```

9
10 SUBROUTINE CLOUDSC &
11 !---input
12 & (KIDIA, KFDIA, KLON, KLEV, &
13 & PTSPHY,&
14 & PT, PQ, tendency_cml,tendency_tmp,tendency_loc, &
15 & PVFA, PVFL, PVFI, PDYNA, PDYNL, PDYNI, &
16 & PHRSW, PHRLW,&
17 & PVERVEL, PAP, PAPH,&
18 & PLSM, LDCUM, KTYPE, &
19 & PLU, PLUDE, PSNDE, PMFU, PMFD,&
20 !---prognostic fields
21 & PA,&
22 & PCLV, &
23 & PSUPSAT,&
24 !-- arrays for aerosol-cloud interactions
25 !!! & PQAER, KAER, &
26 & PLCRIT_AER,PICRIT_AER,&
27 & PRE_ICE,&
28 & PCCN, PNICE,&
29 !---diagnostic output
30 & PCOVPTOT, PRAINFRAC_TOPRFZ,&
31 !---resulting fluxes
32 & PFSQLF, PFSQIF, PFCQNG, PFCQLNG,&
33 & PFSQRF, PFSQSF, PFCQRNG, PFCQSNG,&
34 & PFSQLTUR, PFSQITUR, &
35 & PFPLSL, PFPLSN, PFHPSL, PFHPSN, KFLDX, &
36 & YDCST, YDTHF, YDECLDP)
  
```

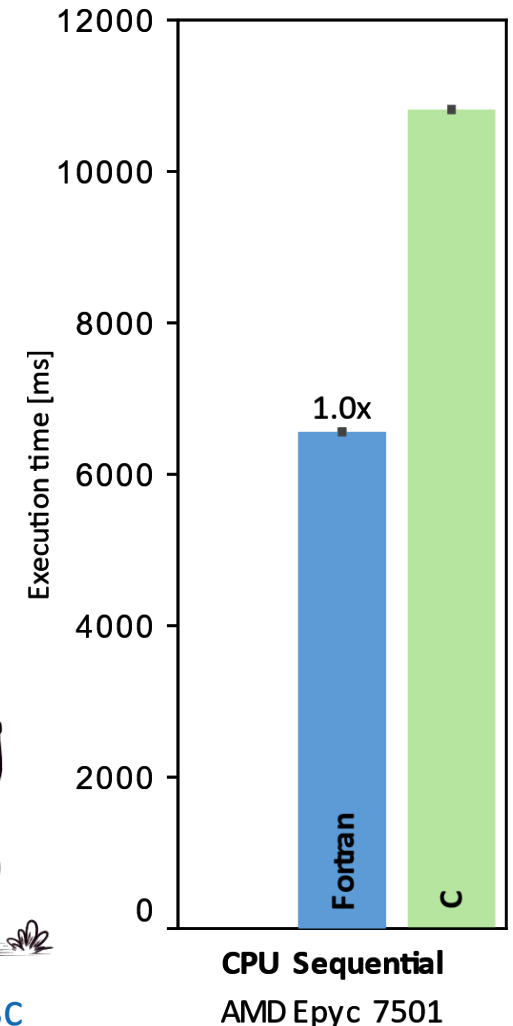
... variable setup/initialization until line 500 ;-)

- **Cloud Microphysics of IFS**
 - Resolve sub-grid features
 - Original 2,525 SLOC of **Fortran 95**

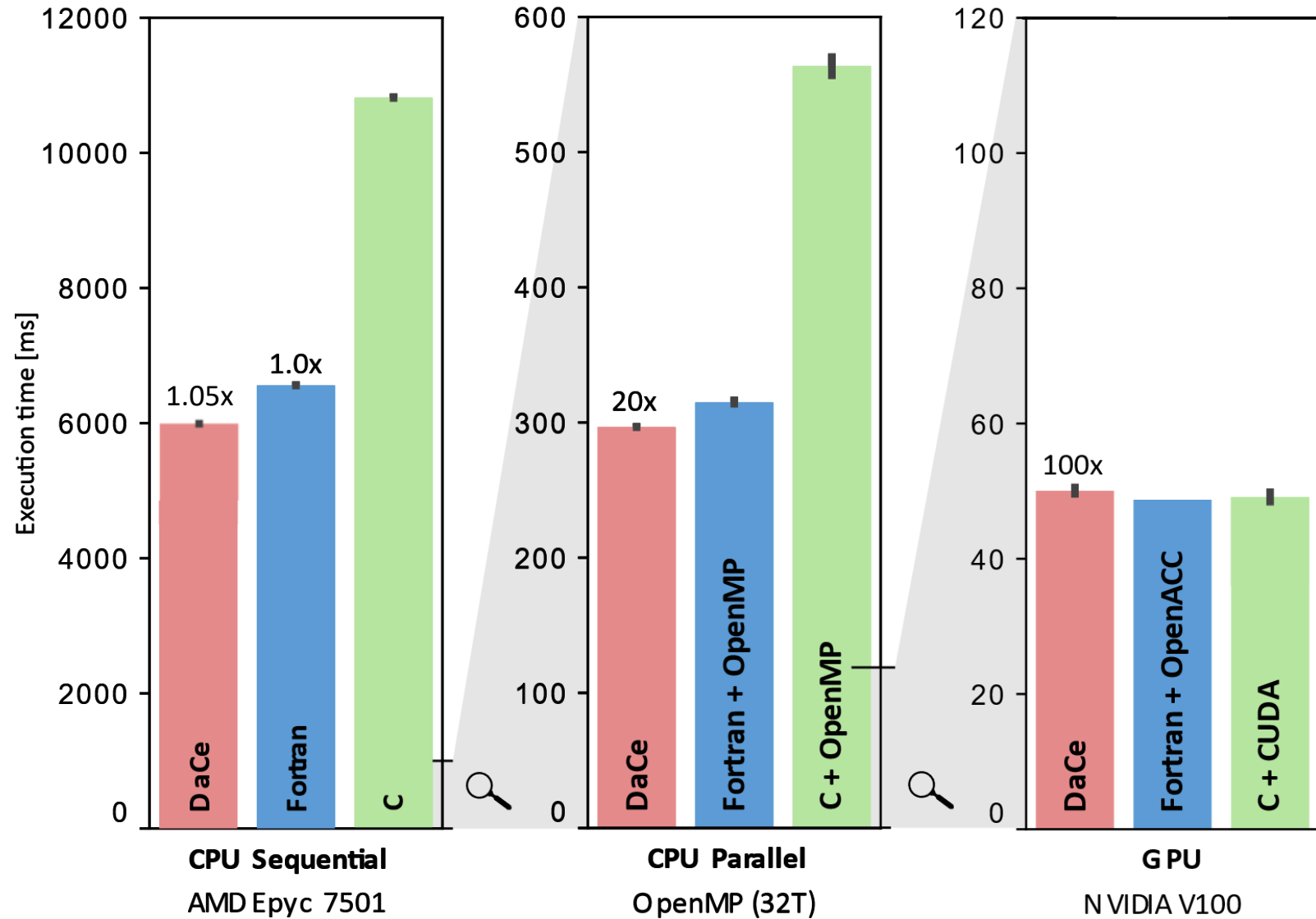
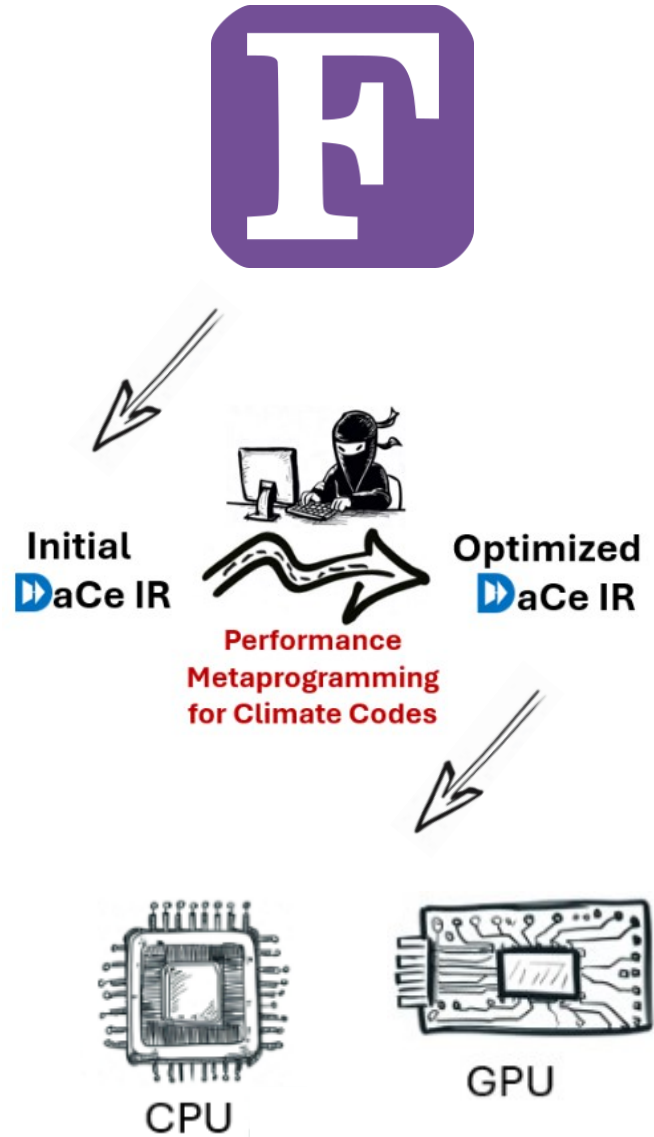
- **Rewritten for performance portability benchmarking (optimization took months!)**
 - 2,635 SLOC C
 - 2,610 SLOC C++/CUDA



<https://github.com/ecmwf-ifs/dwarf-p-cloudsc>

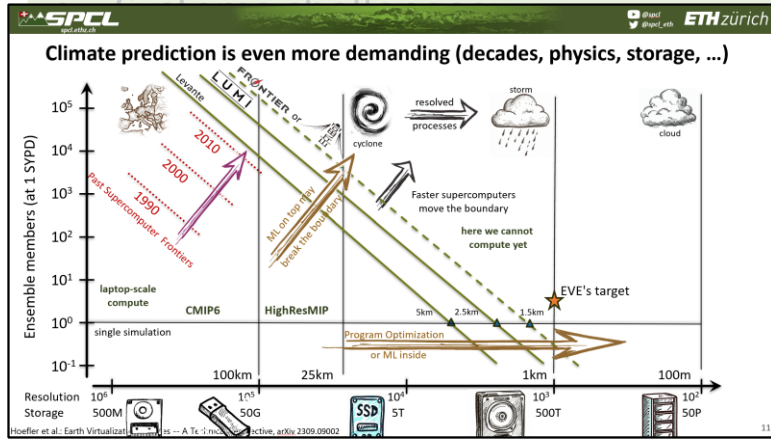


Performance Metaprogramming – from the unchanged CLOUDSC Fortran code!

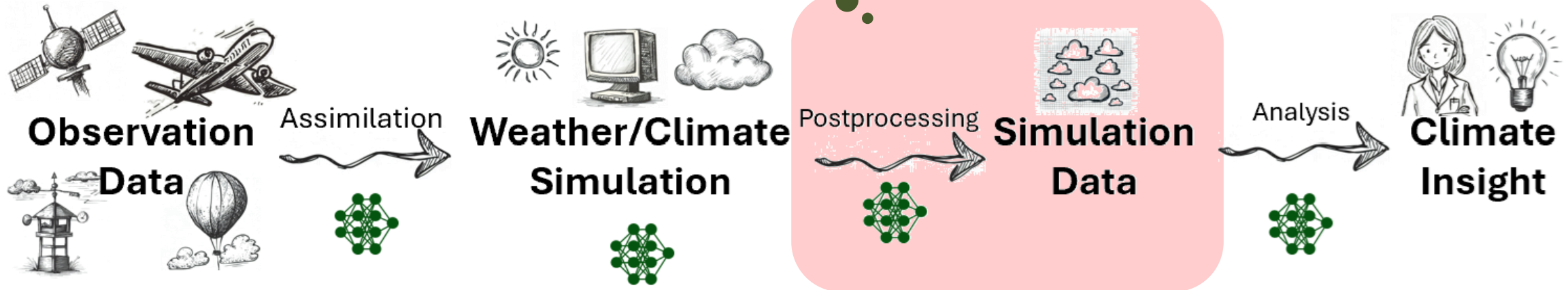
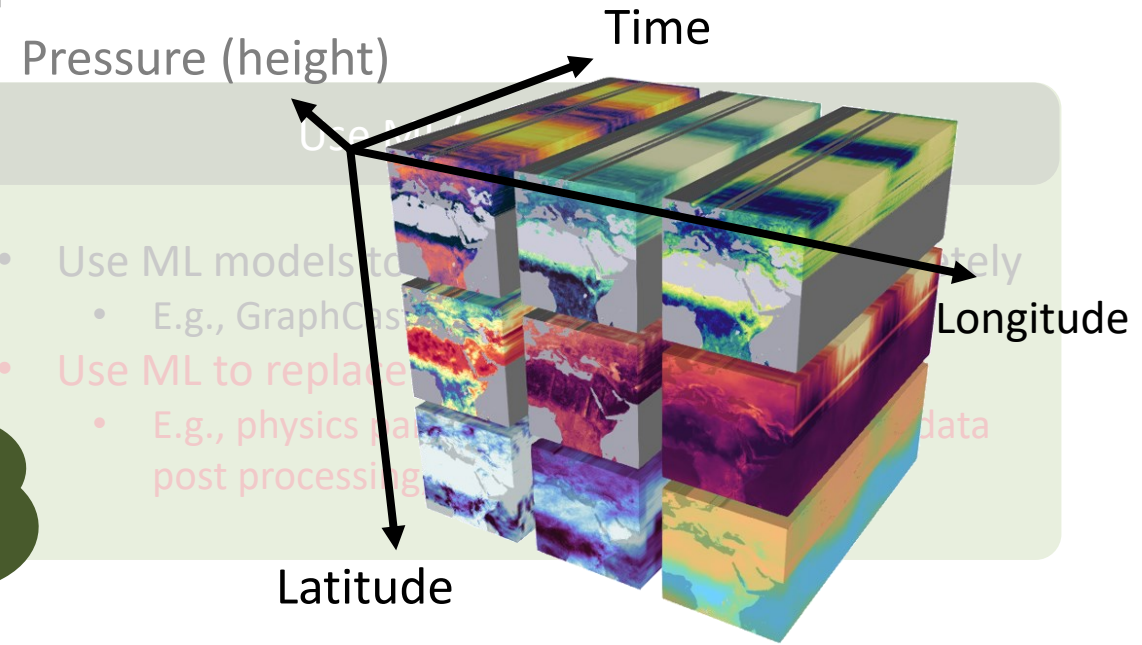


Embracing the future of accelerated computation

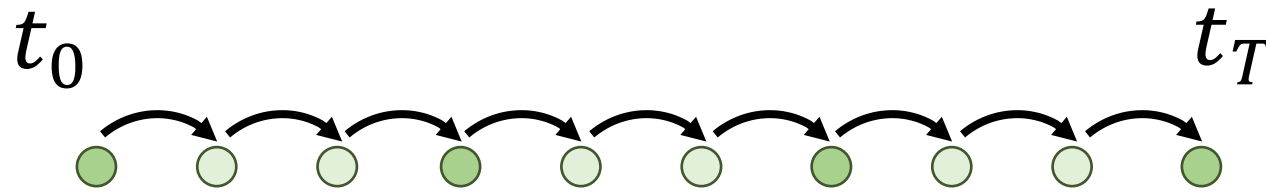
Accelerate Simulations on ML/AI Hardware



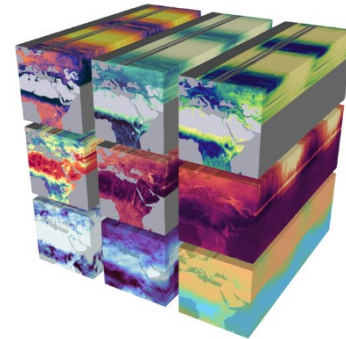
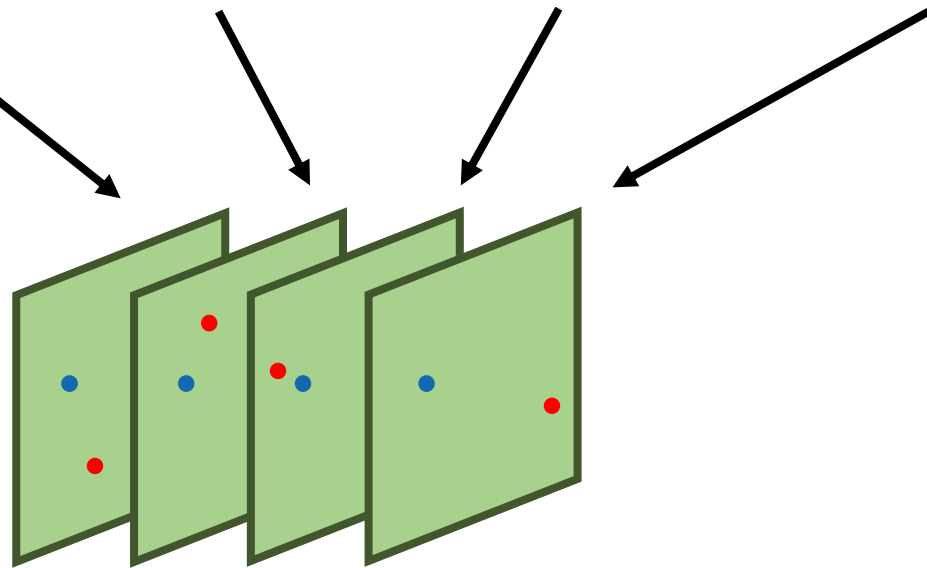
"ML on top"



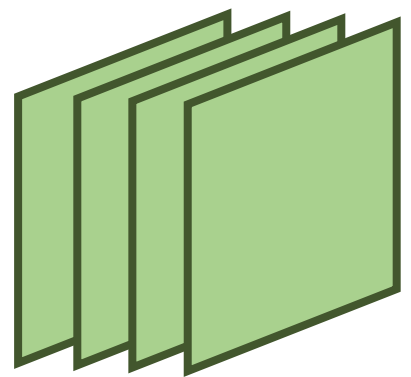
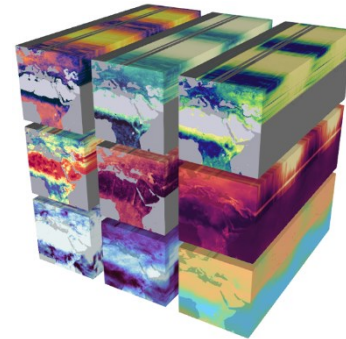
Simulation runs time-stepping forward



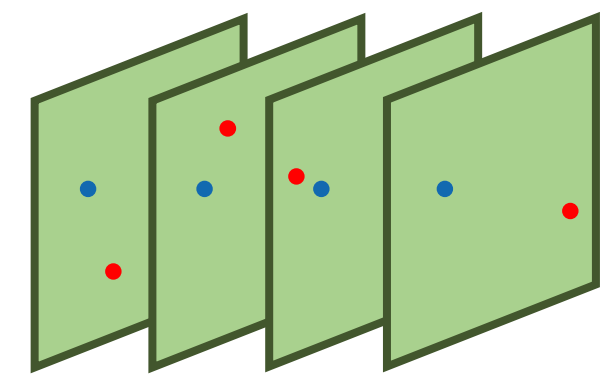
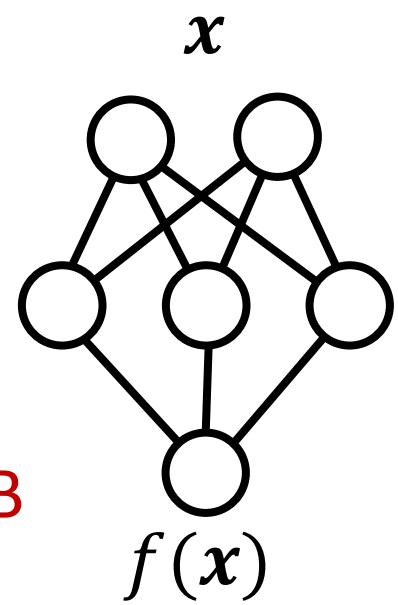
Store some timesteps!



Analysis access pattern is often **strided** or even **random**



Compress/Train
300 x – 3,000 x
15.6GB → 13.8MB

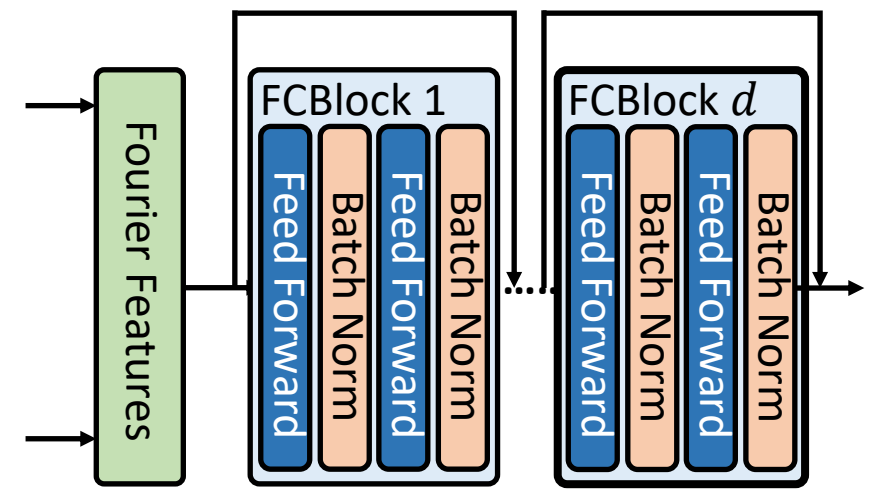
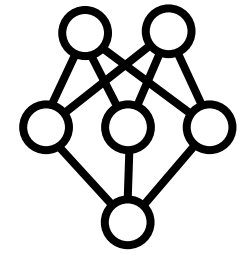


Multidimensional Data

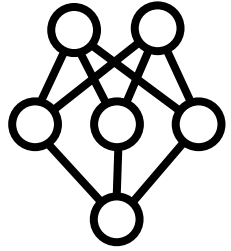
Neural Representation

Analysis Queries

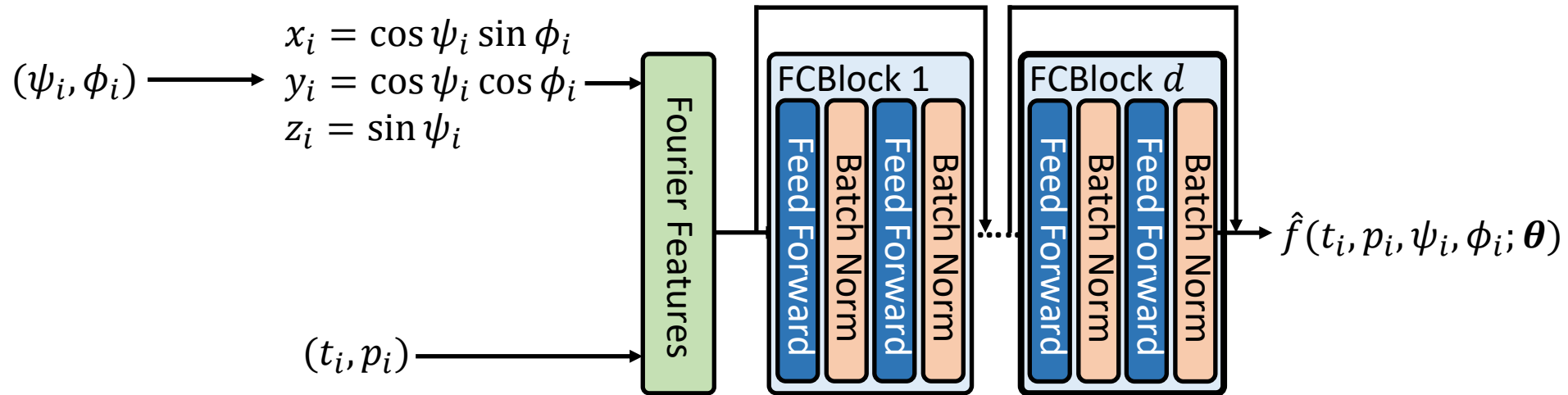
Neural Network Structure



Neural Network Structure

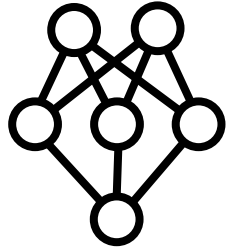


Decompression / Inference

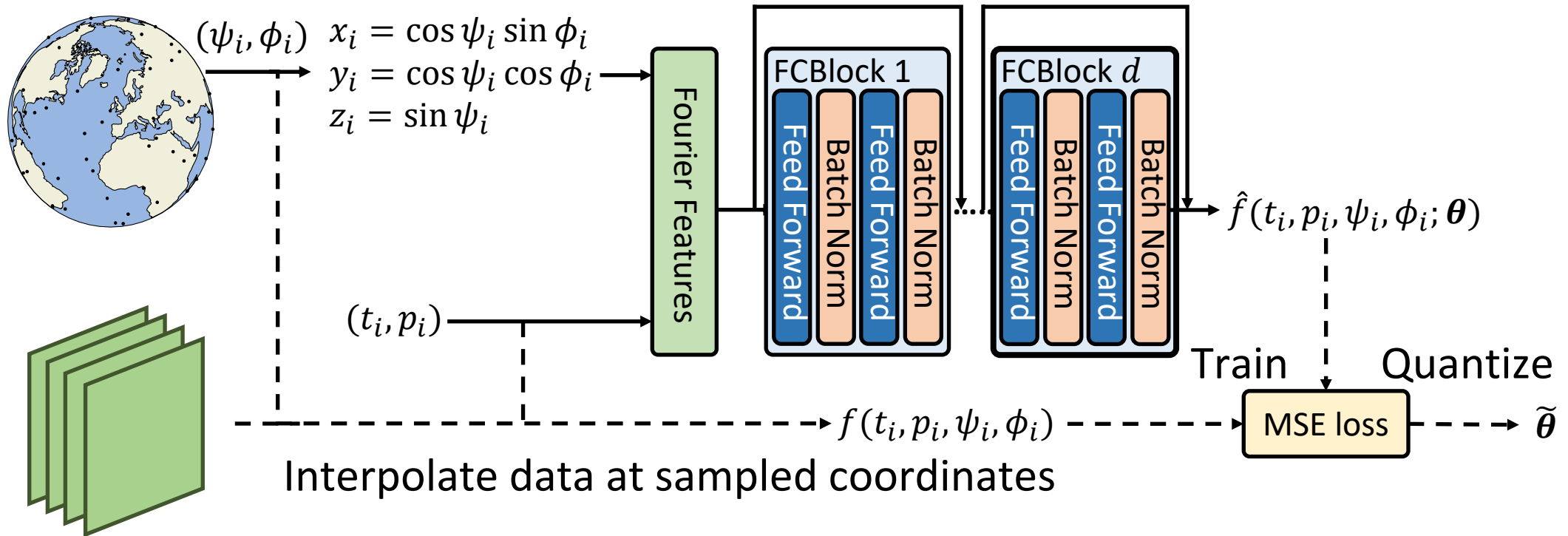


- On-demand decompression
- Fully utilize GPUs

Neural Network Structure

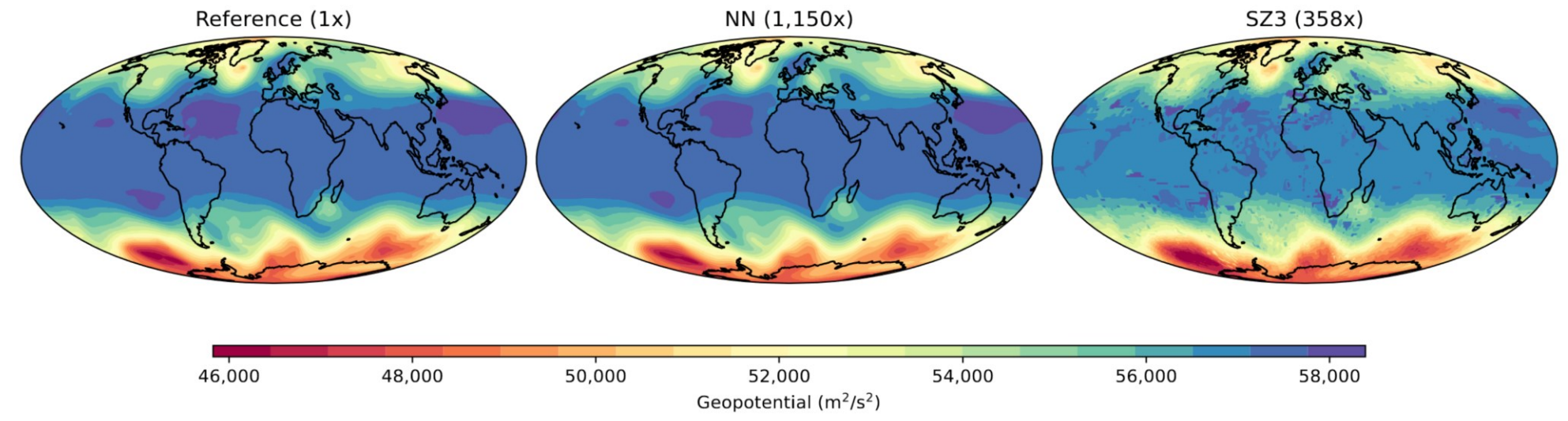


Compression / Training



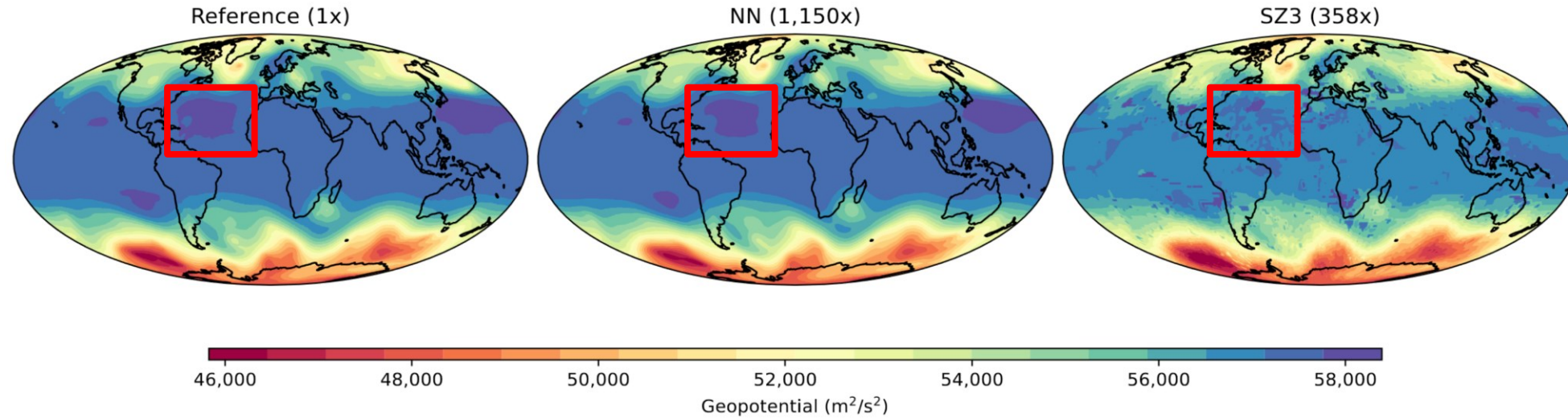
Evaluation: Case Study

Geopotential at 500hPa, 2016 Oct 5th



Evaluation: Case Study

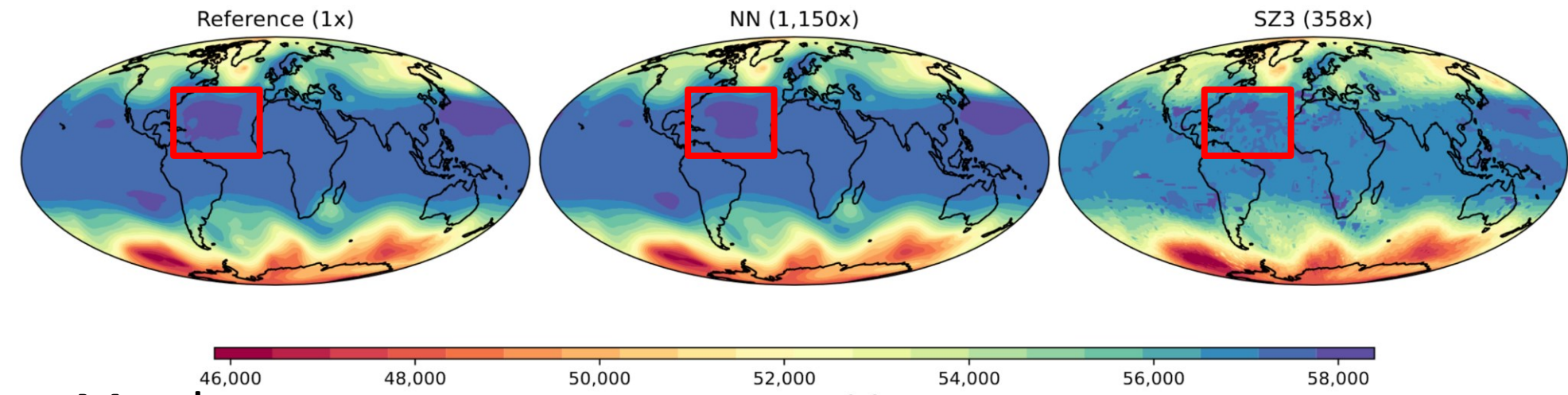
Geopotential at 500hPa, 2016 Oct 5th



Preserves general shapes of important events and average values without introducing significant artifacts

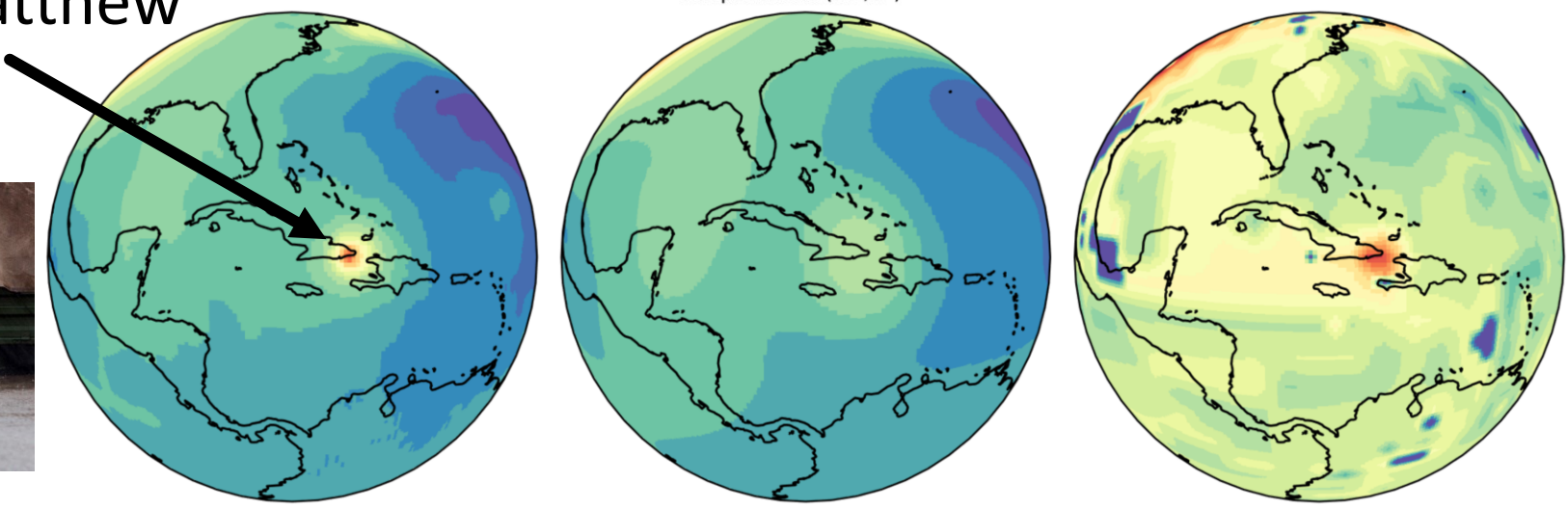
Evaluation: Case Study

Geopotential at 500hPa, 2016 Oct 5th



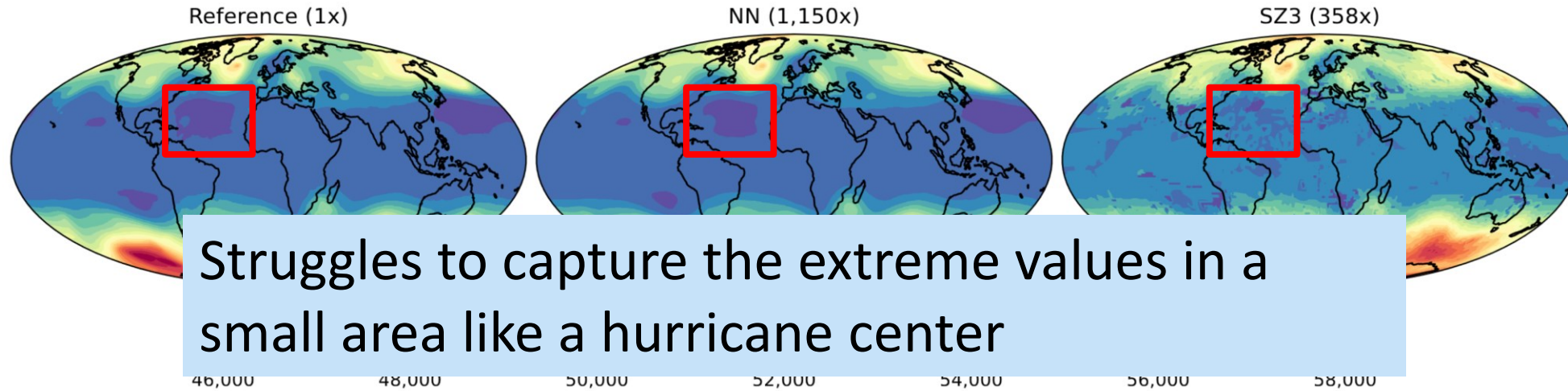
Hurricane Matthew

16.5bn damage
603 fatalities



Evaluation: Case Study

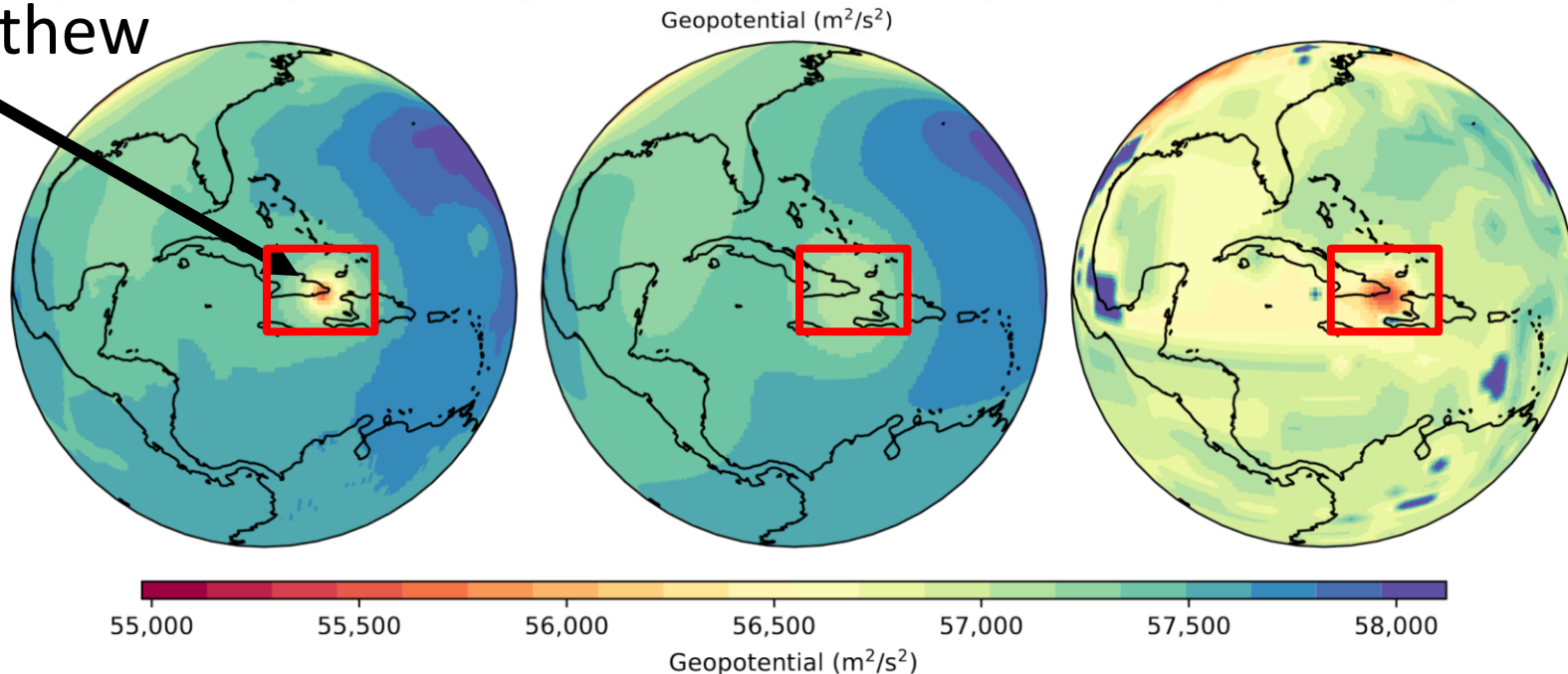
Geopotential at 500hPa, 2016 Oct 5th



Struggles to capture the extreme values in a small area like a hurricane center

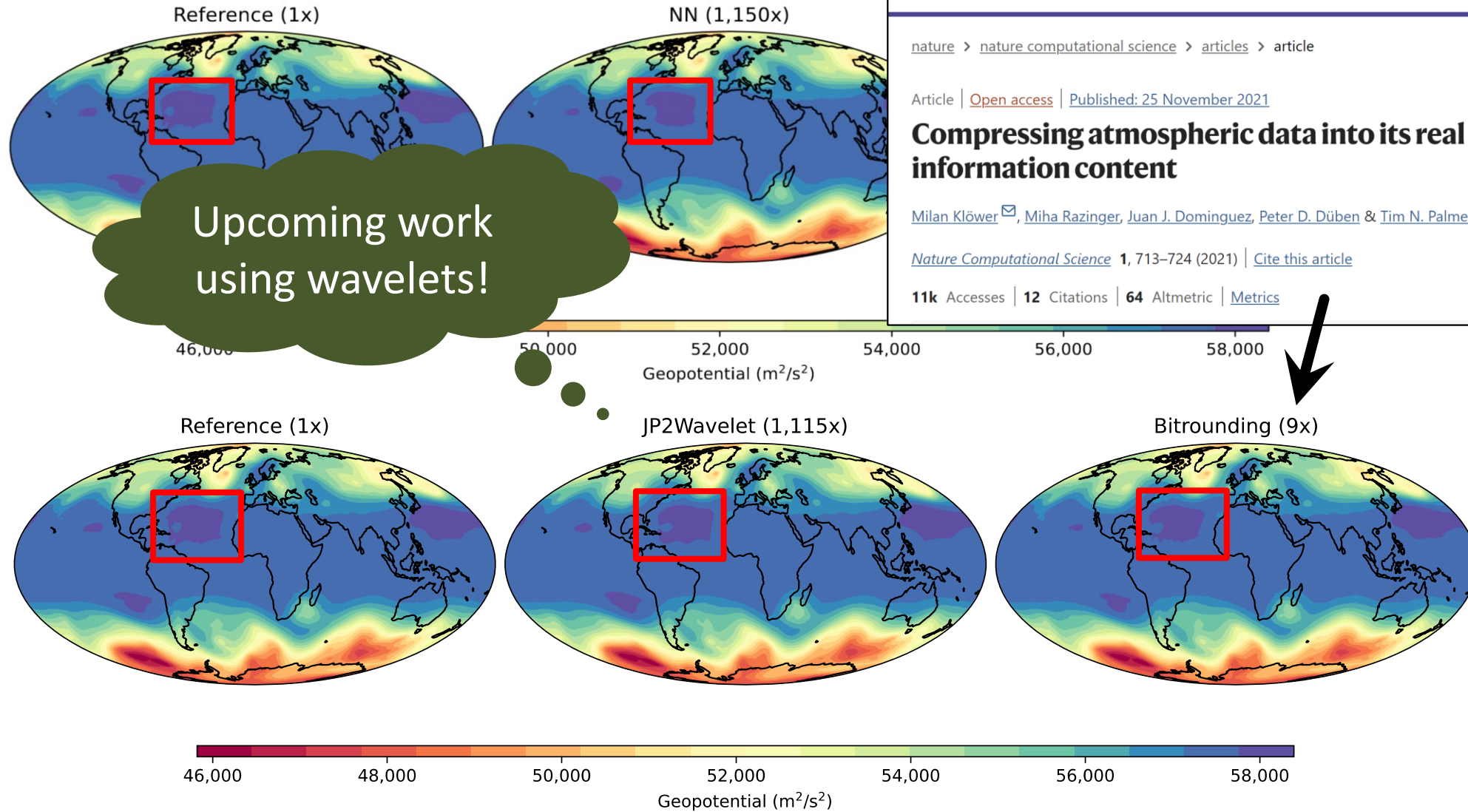
Hurricane Matthew

16.5bn damage
603 fatalities



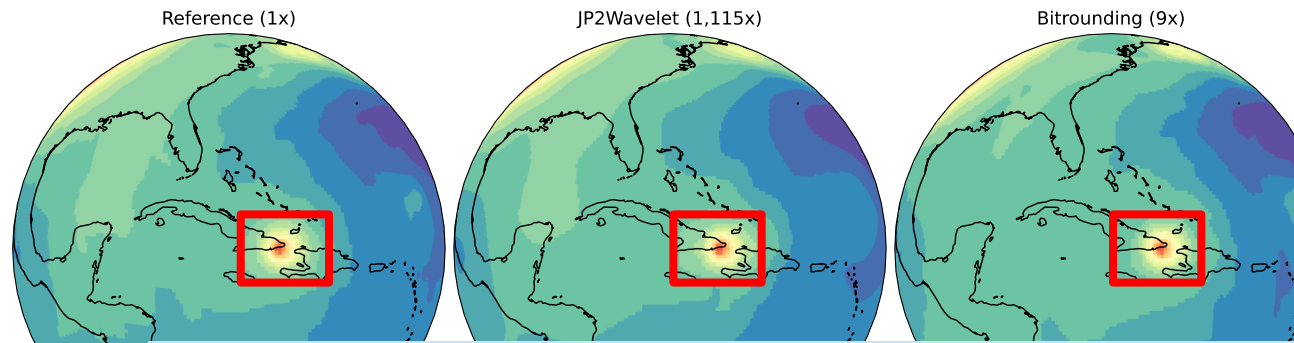
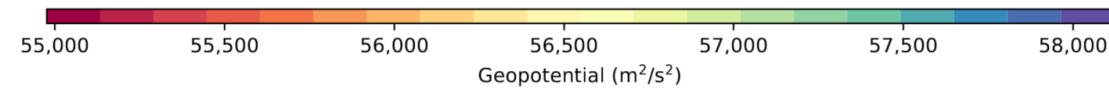
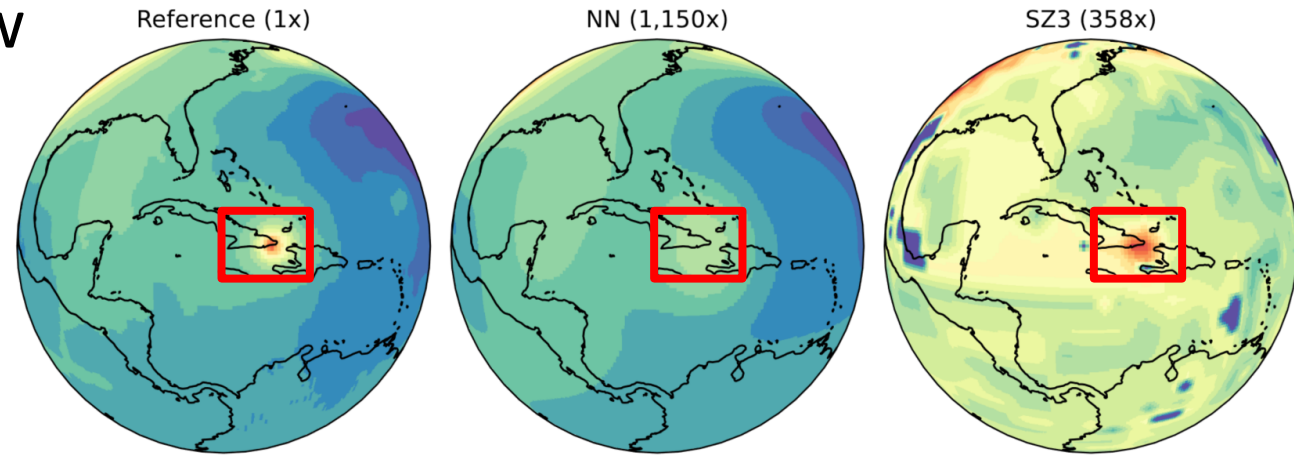
Evaluation: Case Study

Geopotential at 500hPa, 2016

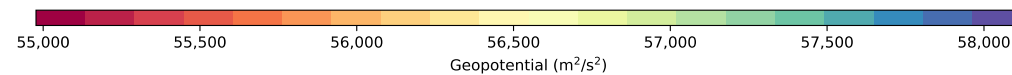


Evaluation: Case Study

Hurricane Matthew



Preserves extreme values at high compression ratio




Summary and Key Points

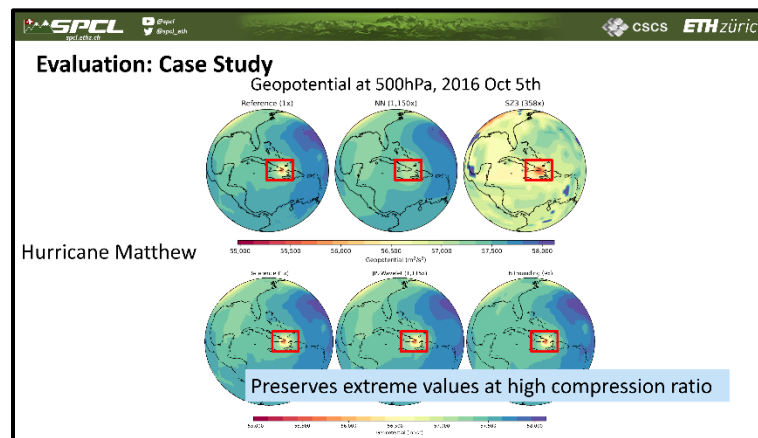
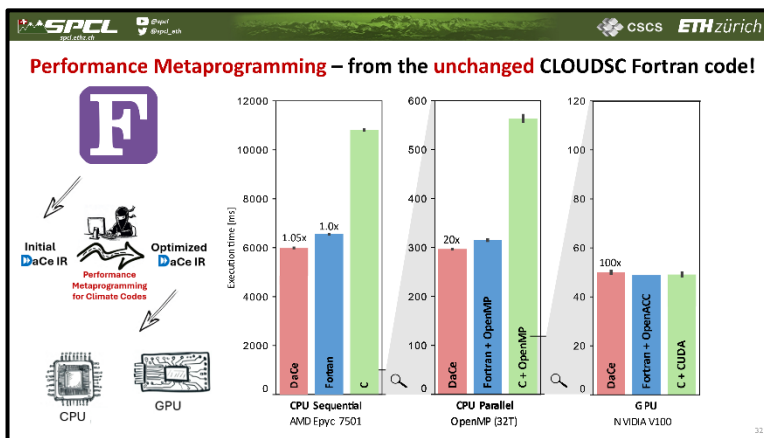
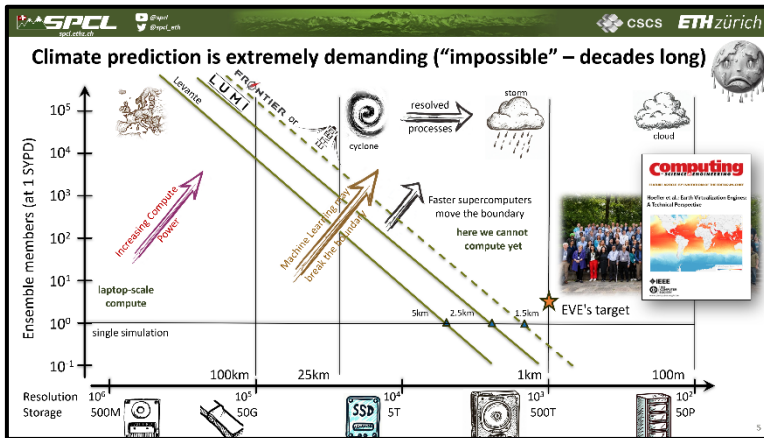
More of SPCL's research:

 youtube.com/@spcl  150+ Talks

 twitter.com/spcl_eth  1.2K+ Followers

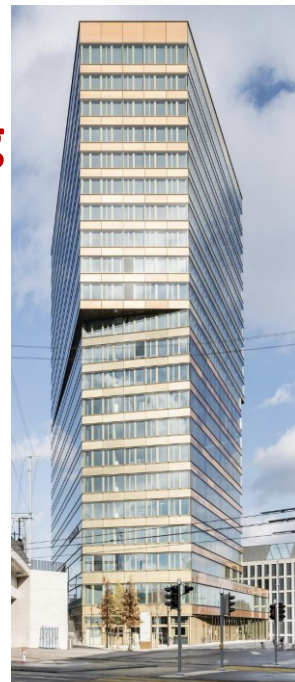
 github.com/spcl  2K+ Stars

... or spcl.ethz.ch



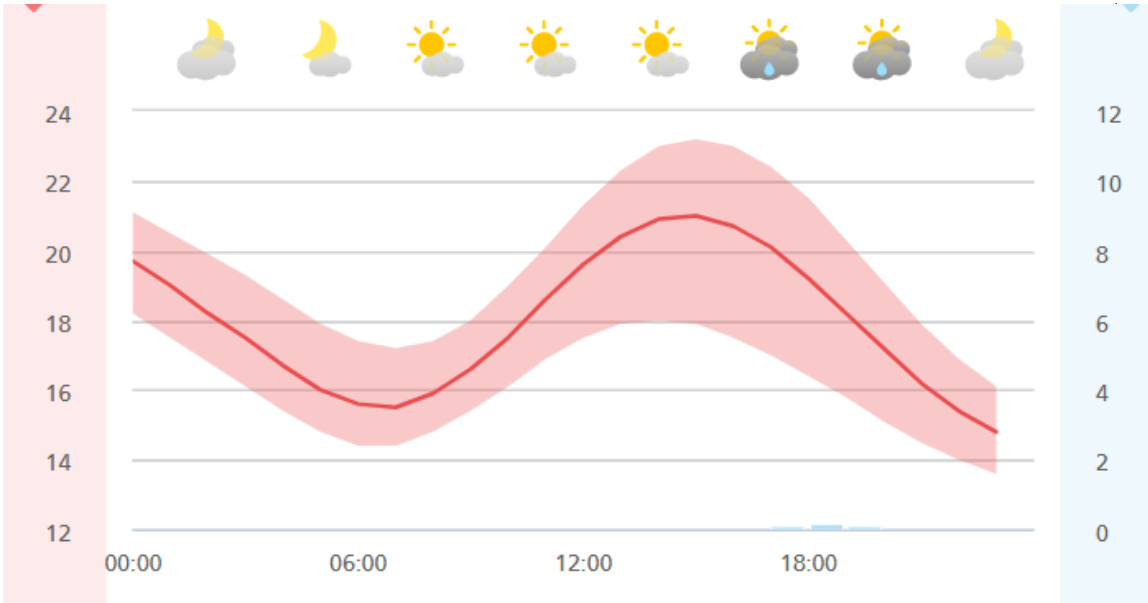
Join us! We're looking for PhD students, postdocs, and academic visitors in Zurich!

<http://spcl.ethz.ch/Jobs/>
<http://spcl.ethz.ch/Visit/>

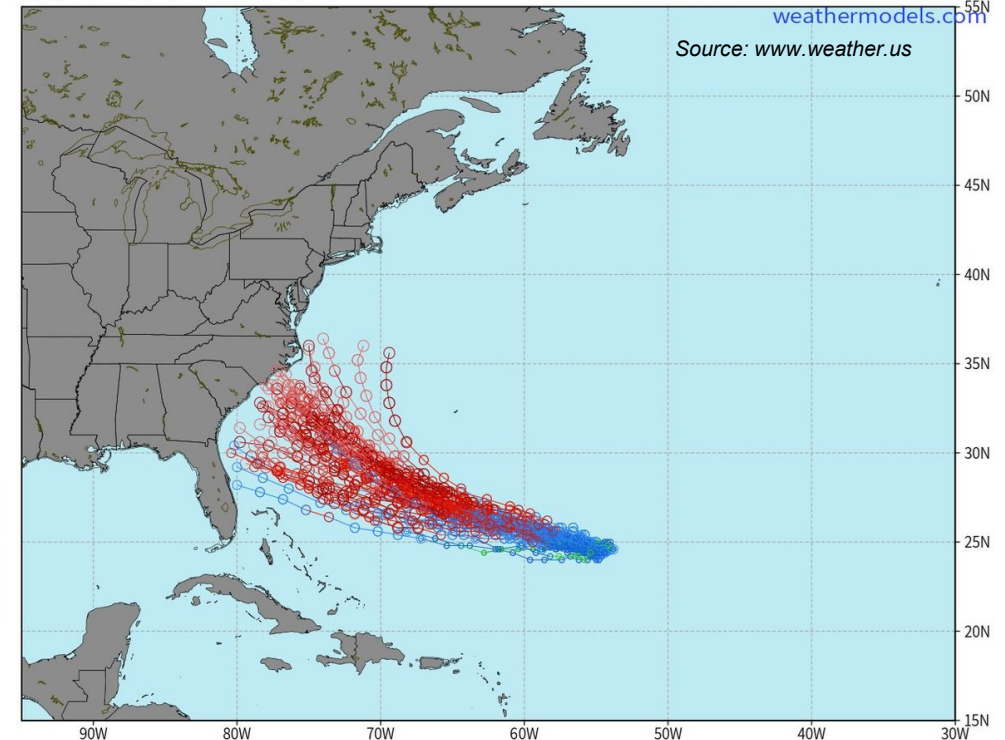


All of ERA-5 on a USB-drive! Run your own analyses on your laptop!

Uncertainty in forecasting

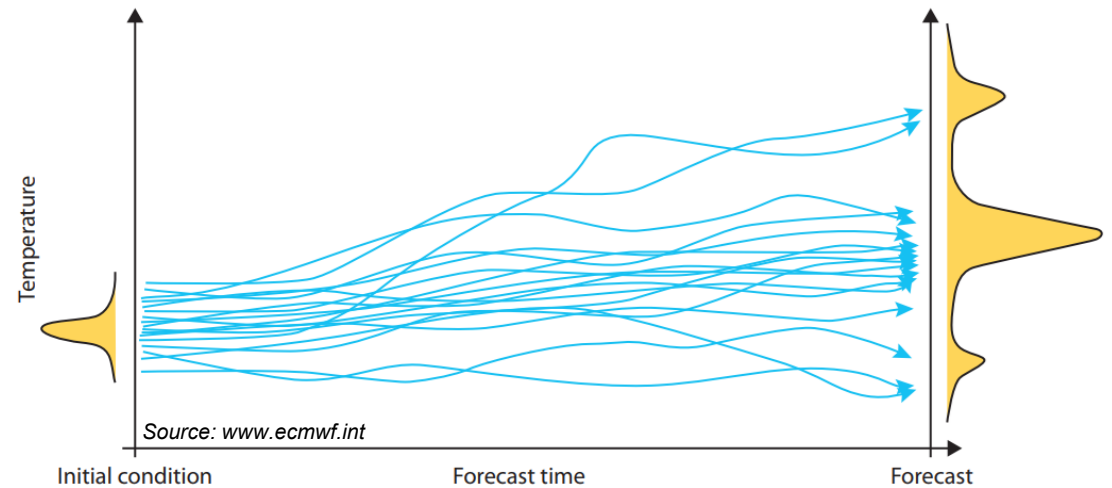


ECMWF EPS Tropical Cyclone Location 06L.FLORENCE --> Next [126] Hours
 INIT: 12Z08SEP2018 --> 18Z13SEP2018



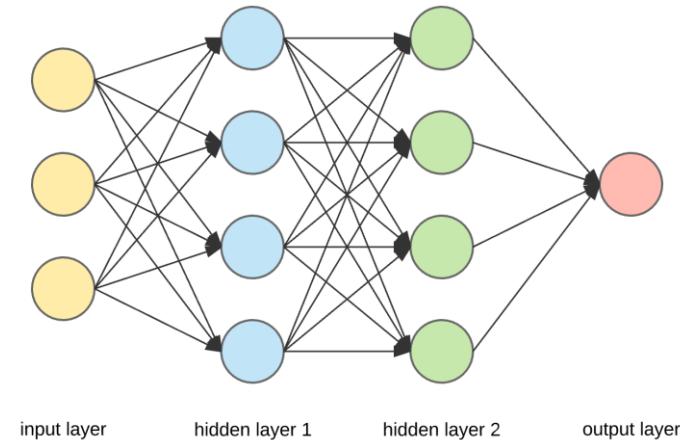
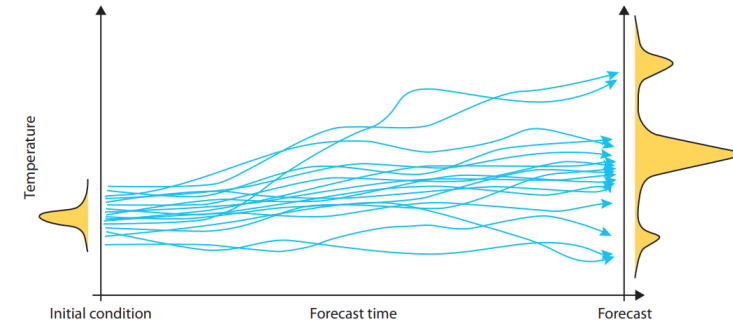
- **Weather is a chaotic system**
 - Minor perturbations affect the outcome the further into the future we predict

- **Solution: Ensemble Prediction Systems – predict weather as a probability distribution**
 - Approximated by partial differential equations with perturbed inputs



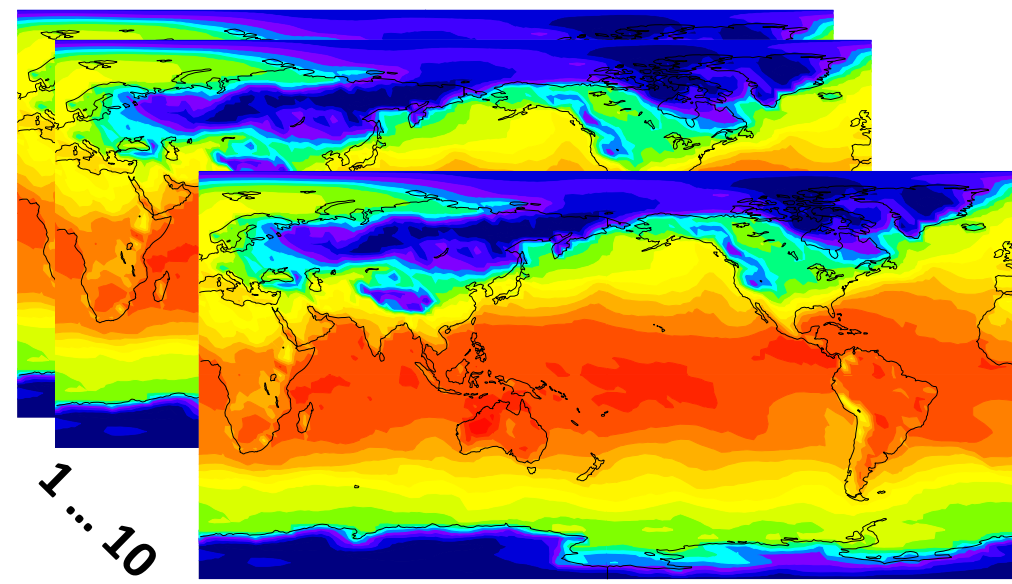
Ensemble Prediction System at ECMWF

- Initial condition uncertainties result from data assimilation of sensor data
- 51 ensemble members, 1 control (deterministic), 50 perturbed (stochastic)
 - Approximate the highest likely trajectory from output distribution D
 - Lower resolution (9km vs. 18km) in order to fit compute budget
mostly an economic argument
- Next step in the economic argument:
 - Could the number of ensemble members be reduced without sacrificing accuracy?
 - **Idea I:** predict mean and standard deviation (StdDev) of D from a smaller ensemble
This may allow us to increase resolution at equal cost – better predictions
 - Can we improve prediction quality by learning from ground truth observations?
 - **Idea II:** learn (local) model bias from observations
This may allow us to increase accuracy – better predictions



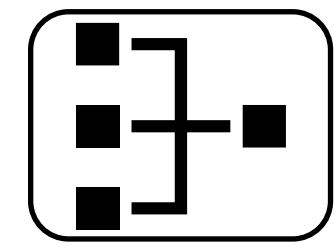
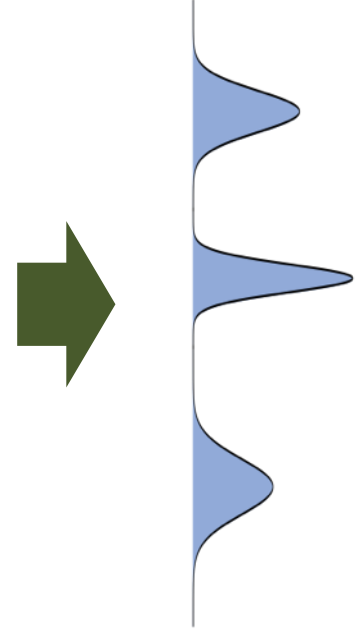
ENS-10: A Dataset For Post-Processing Ensemble Weather Forecasts

Ashkboos et al., NeurIPS'22
(corrected distribution)

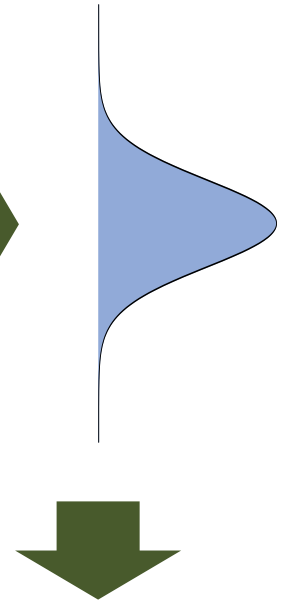


ENS-10

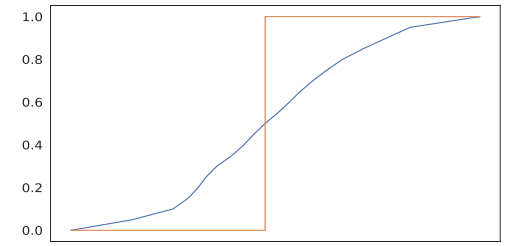
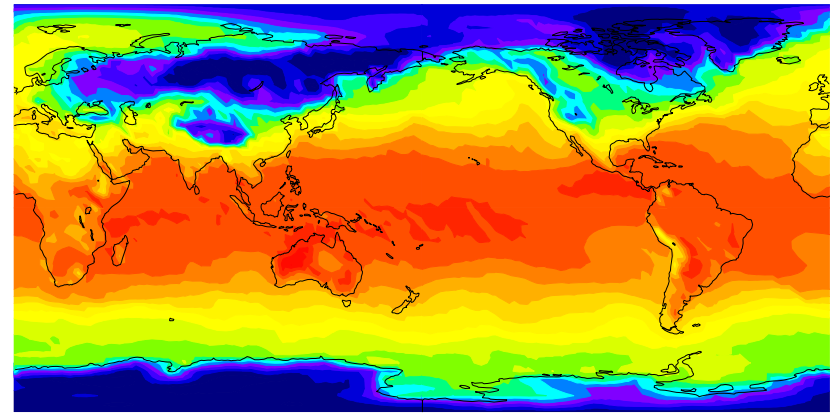
(biased distribution)



(corrected distribution)

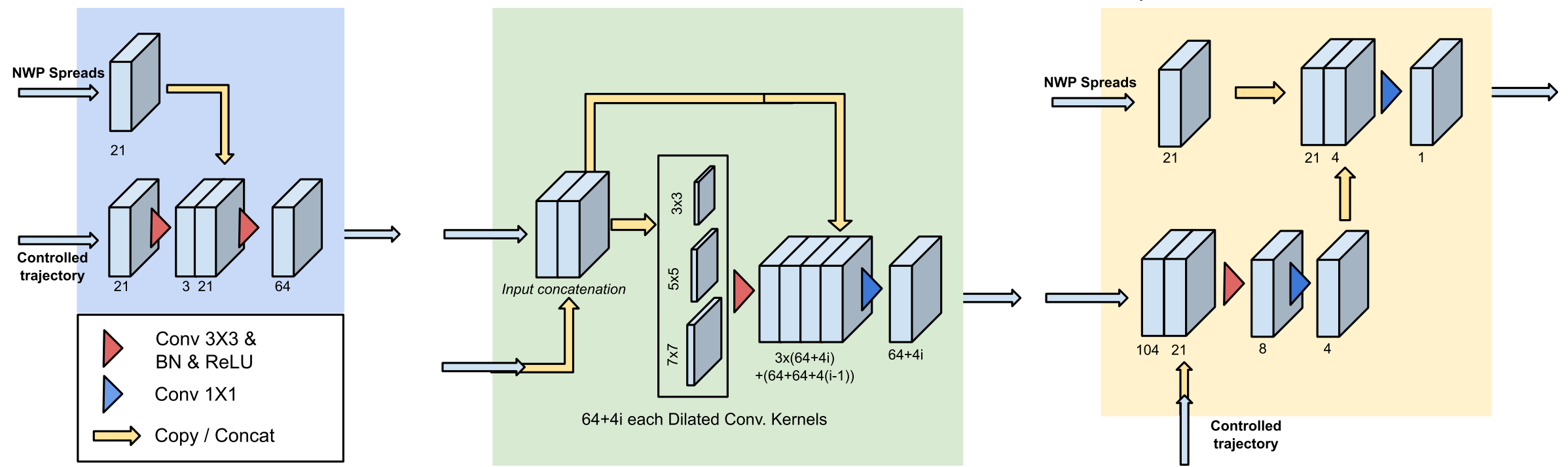
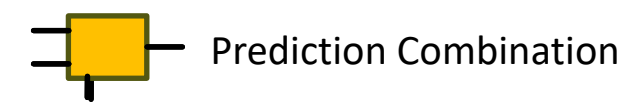
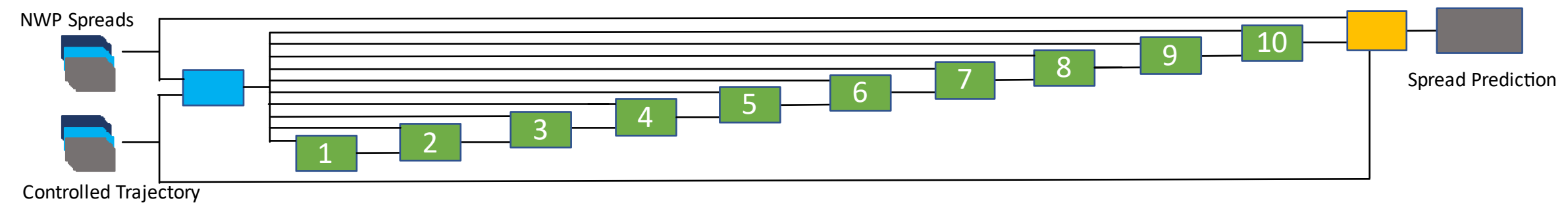


ERA5
(ground truth)

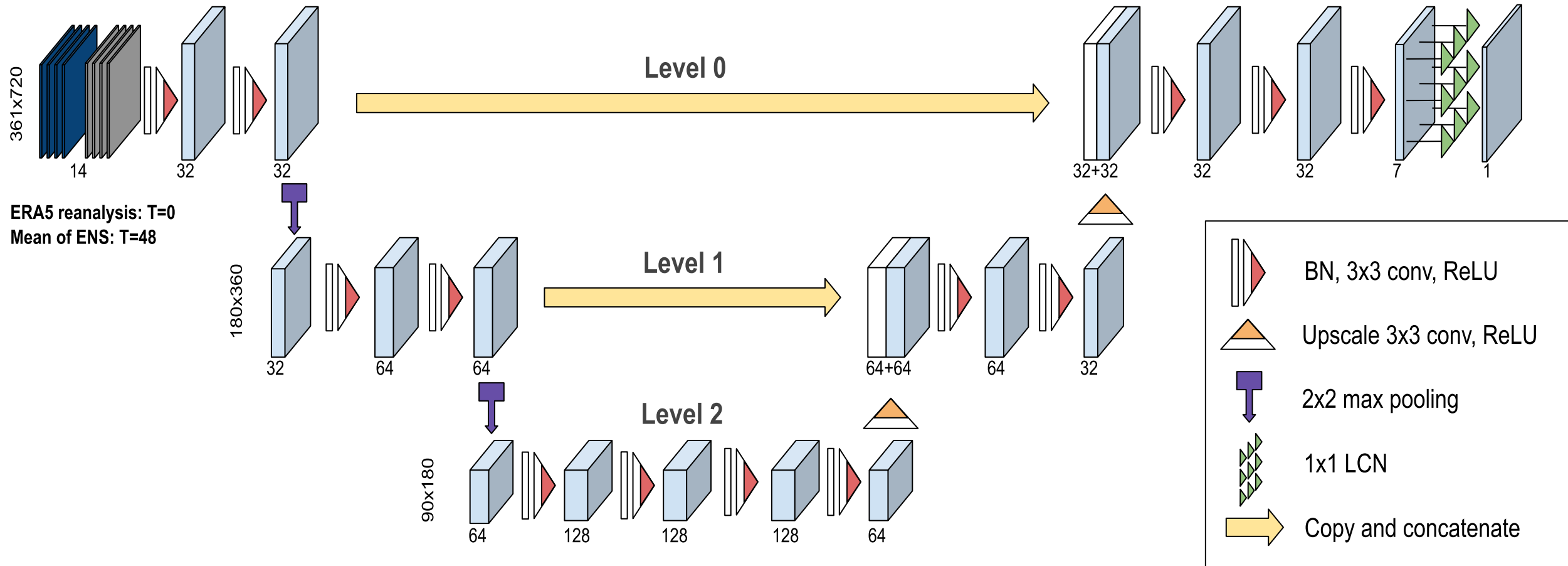


Score

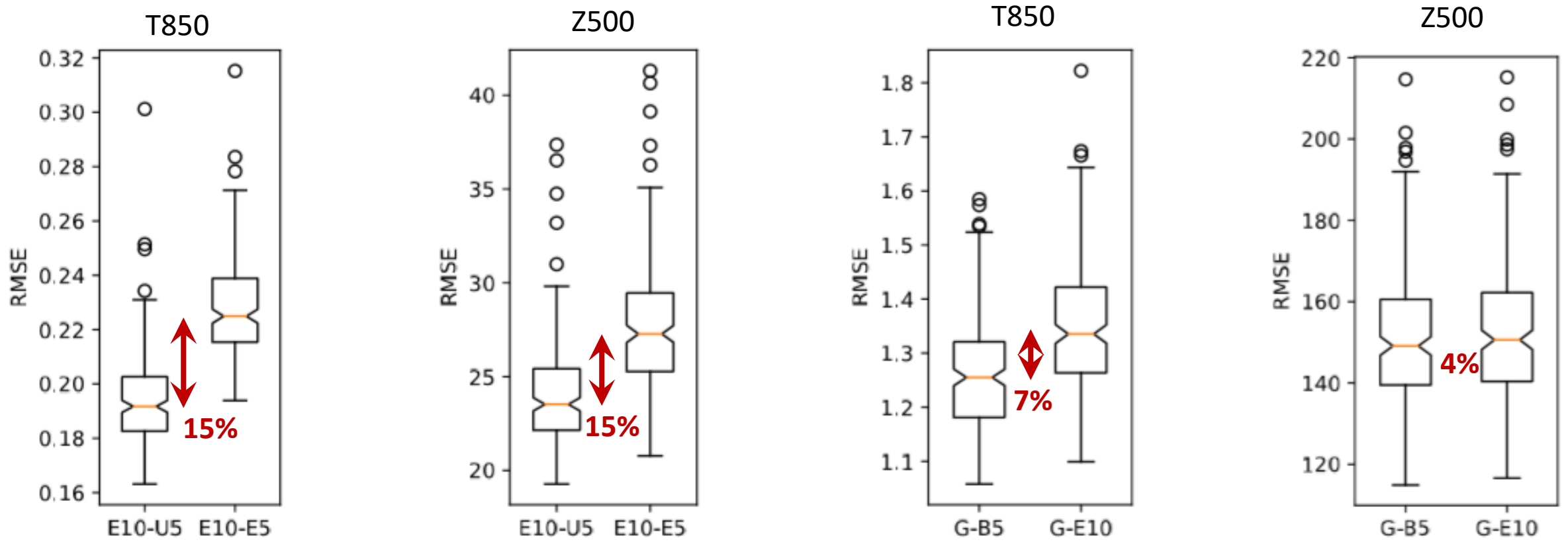
Uncertainty Quantification Network (based on ResNet)



Bias Correction Network (based on 3D-Unet + LCN)



Global RMSE results



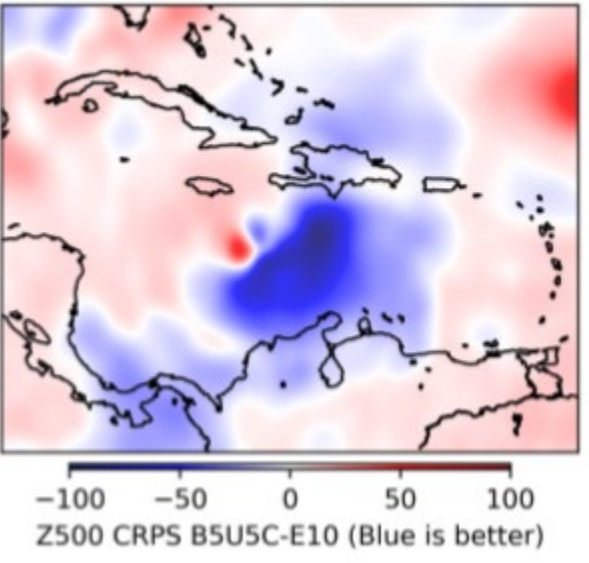
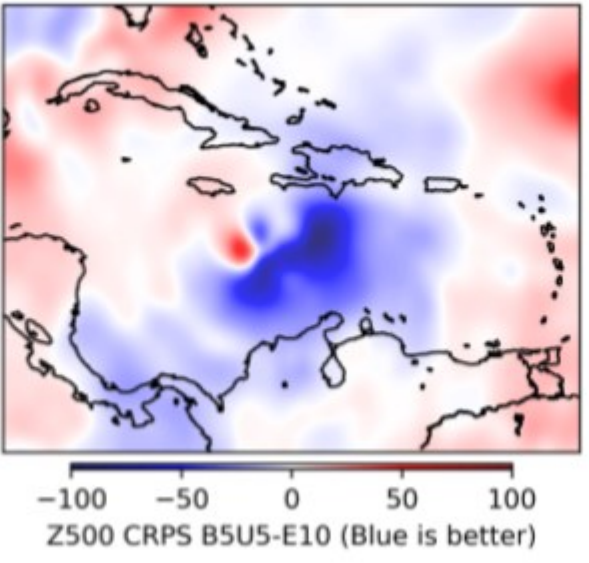
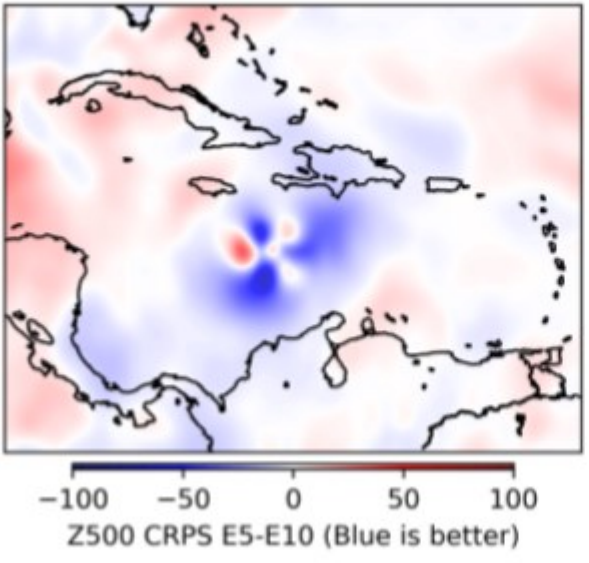
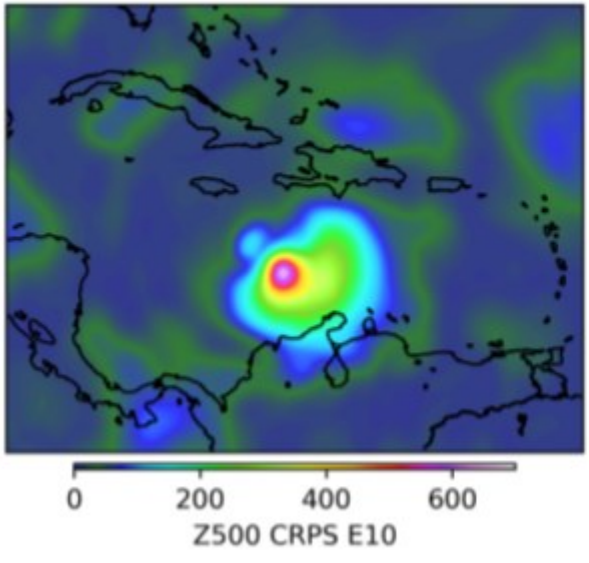
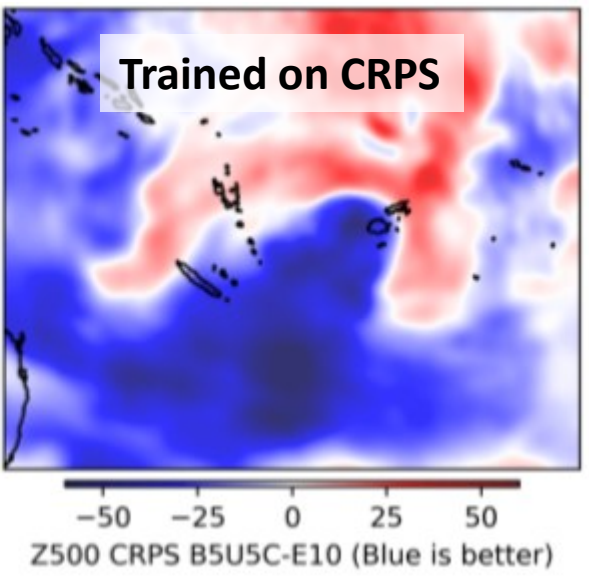
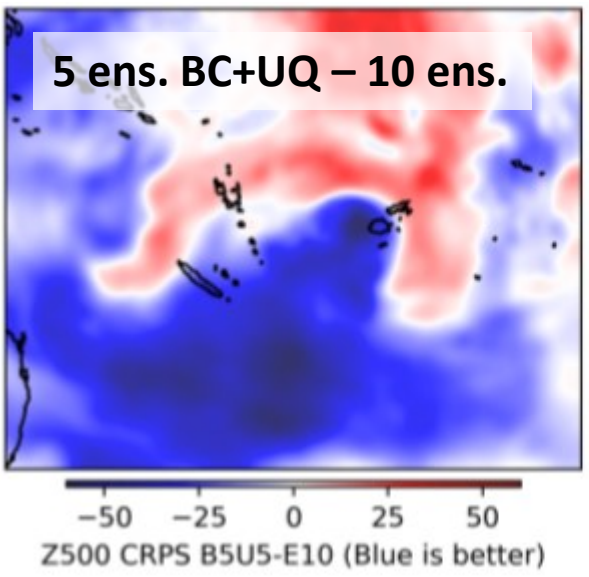
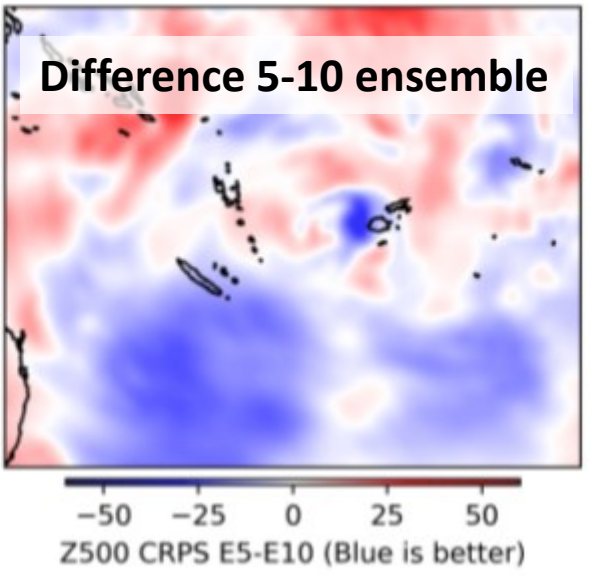
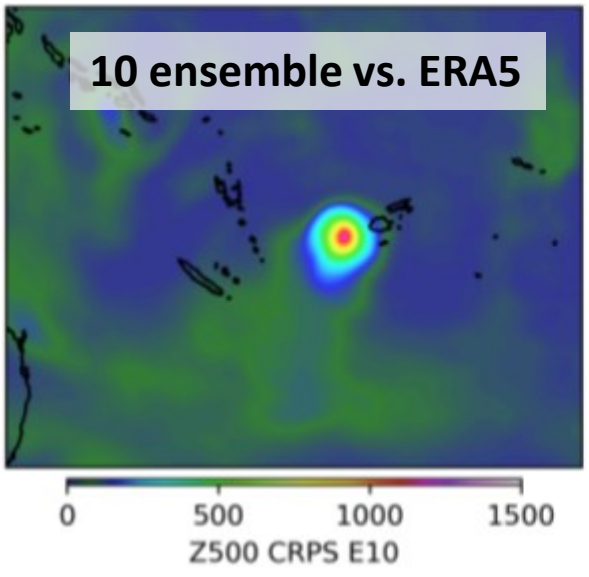
10 ensembles vs. UQ with 5 ensembles

10 ensembles vs. 5 ensembles

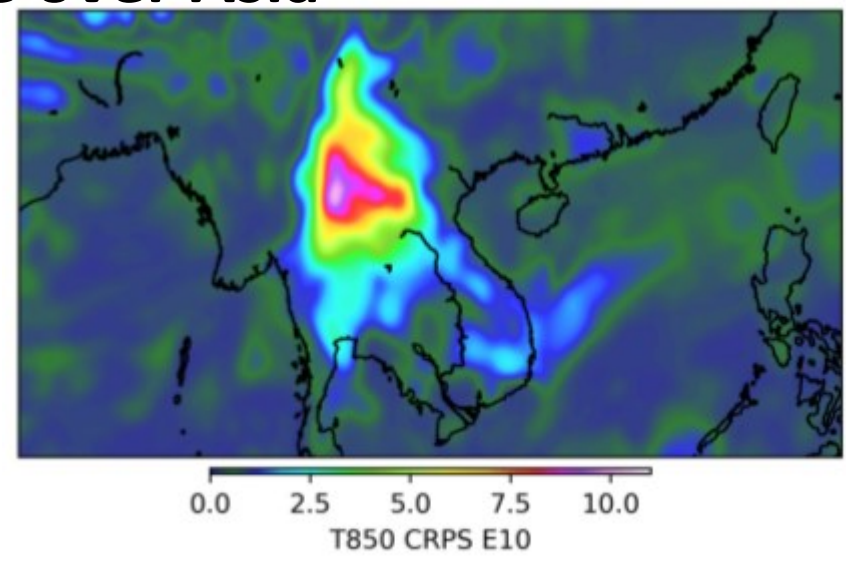
ERA5 (ground truth) vs. BC with 5 trajectories

ERA5 (ground truth) vs. 10 trajectories

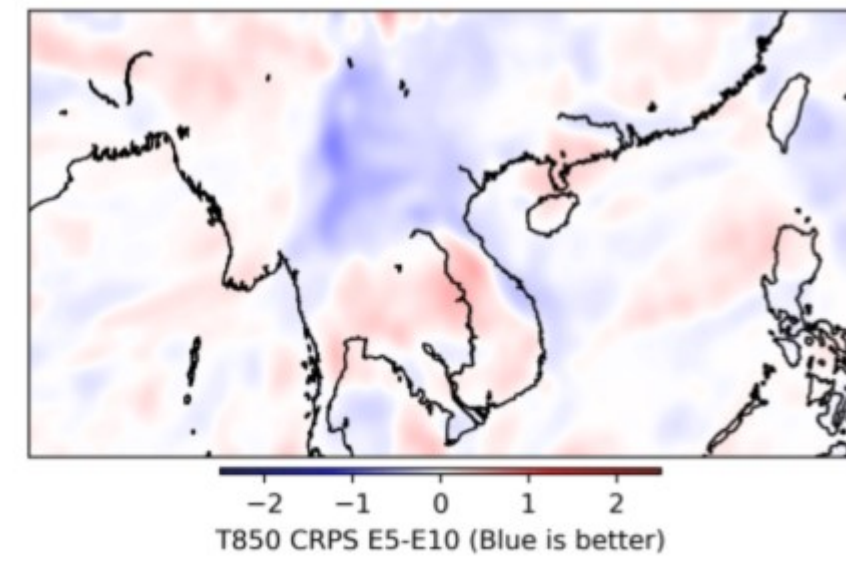
Extreme event: Tropical Cyclone Winston & Hurricane Matthews



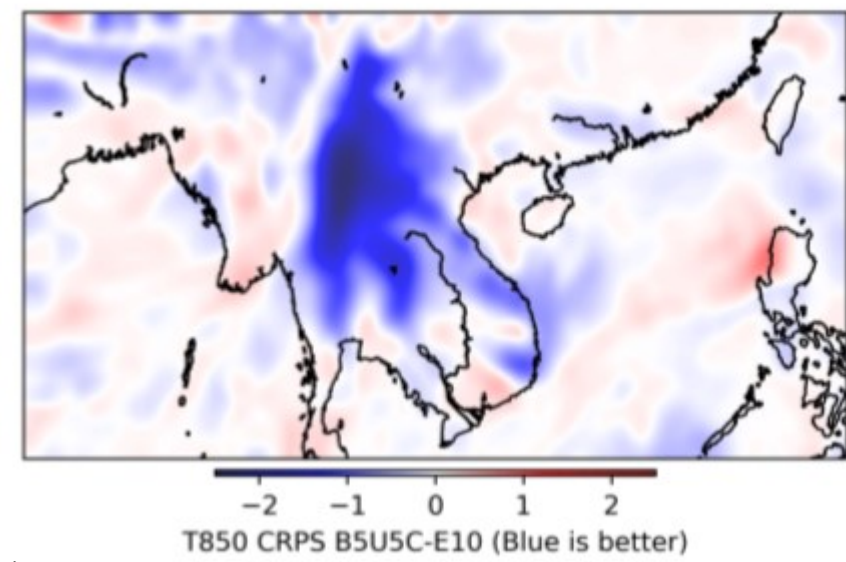
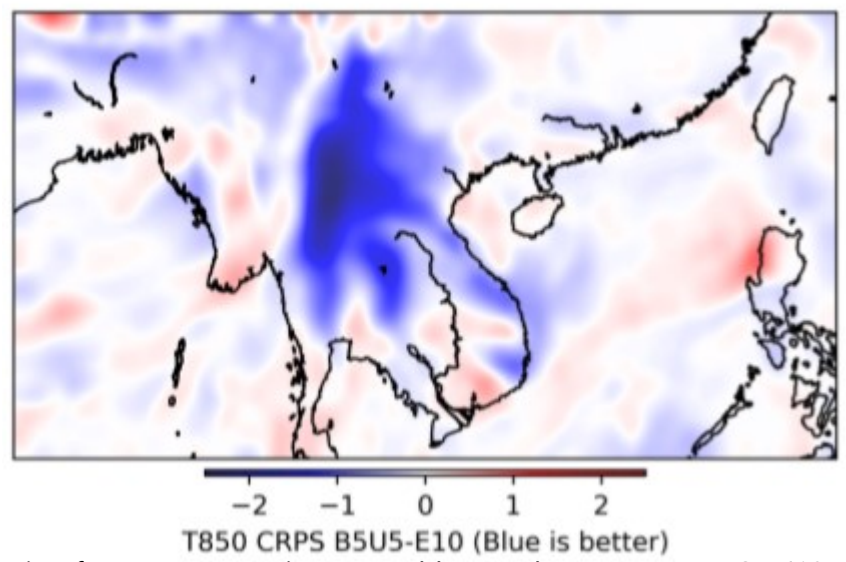
Cold wave over Asia



(a) E10



(b) E5-E10



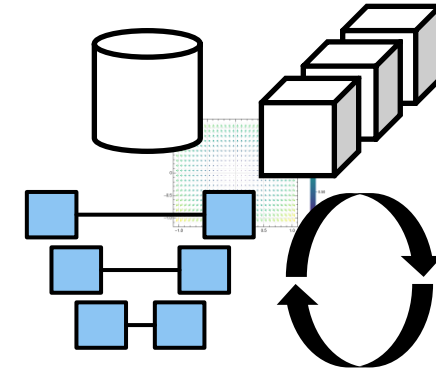
Intermediate Conclusions (Preliminary Study)

- **Simple Deep Learning can be used to accelerate forecast pipelines**
 - Take advantage of industry efforts to tune hardware and tool-chains
 - An informed approach is **necessary** to ensure improved results

- **Using Encoder-Decoder networks for predicting mean and StdDev in ensemble systems yields higher accuracy than using small ensemble statistics**
 - Fewer than half of the ensemble members are necessary
 - Accuracy improved with custom operators

- **Promising for increasing performance in large-scale settings**
 - Needs further investigation!
 - Join us/try yourself: <https://github.com/spcl/deep-weather>

- **Future directions:**
 - Larger datasets
 - Custom neural architectures for unstructured grids
 - Integrate into dace tool-chain for further optimization

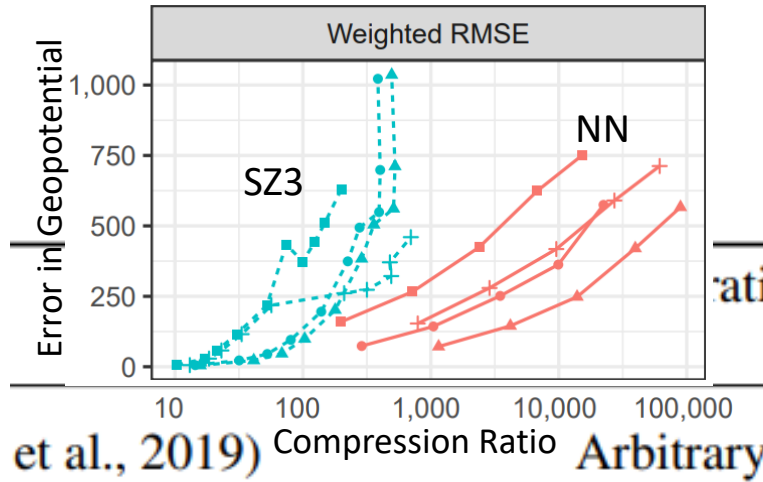
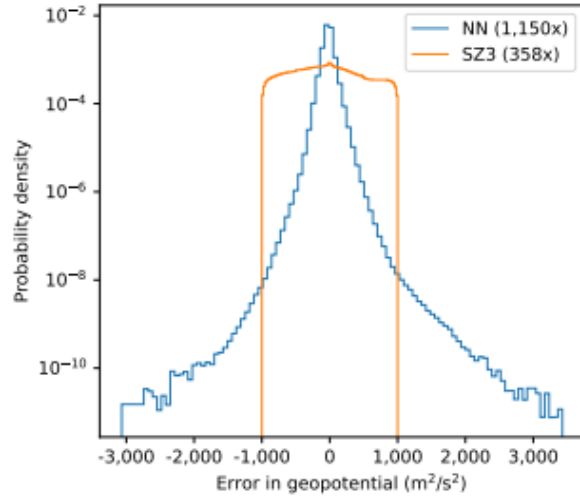


Massive opportunity: Addressing the Climate Data Deluge (arXiv:2210.12538)

- ECMWF soon produces 1PB/day of simulation data – we need to compress it!

- Key idea [1]: **Overfit** a Fourier Network to a block of (climate) data!

Massive opportunity: Addressing the Climate Data Deluge (arXiv:2210.12538)

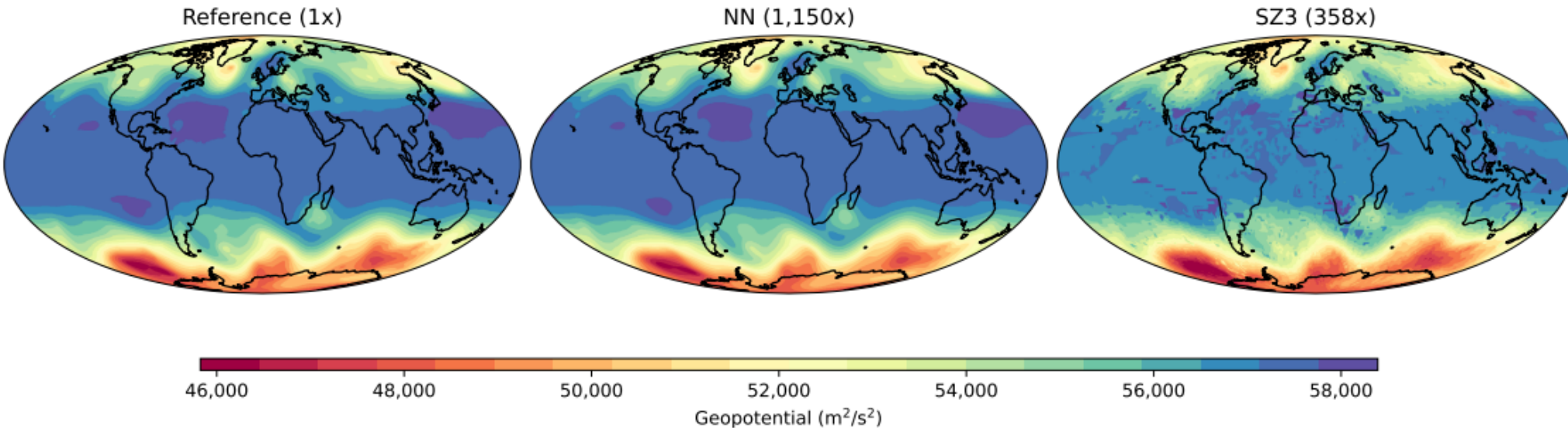


ratio	Comp. speed	Decomp. speed
	Cont.	Rand.



SZ3 enforces strict error bounds... which limits compression $< 10x$

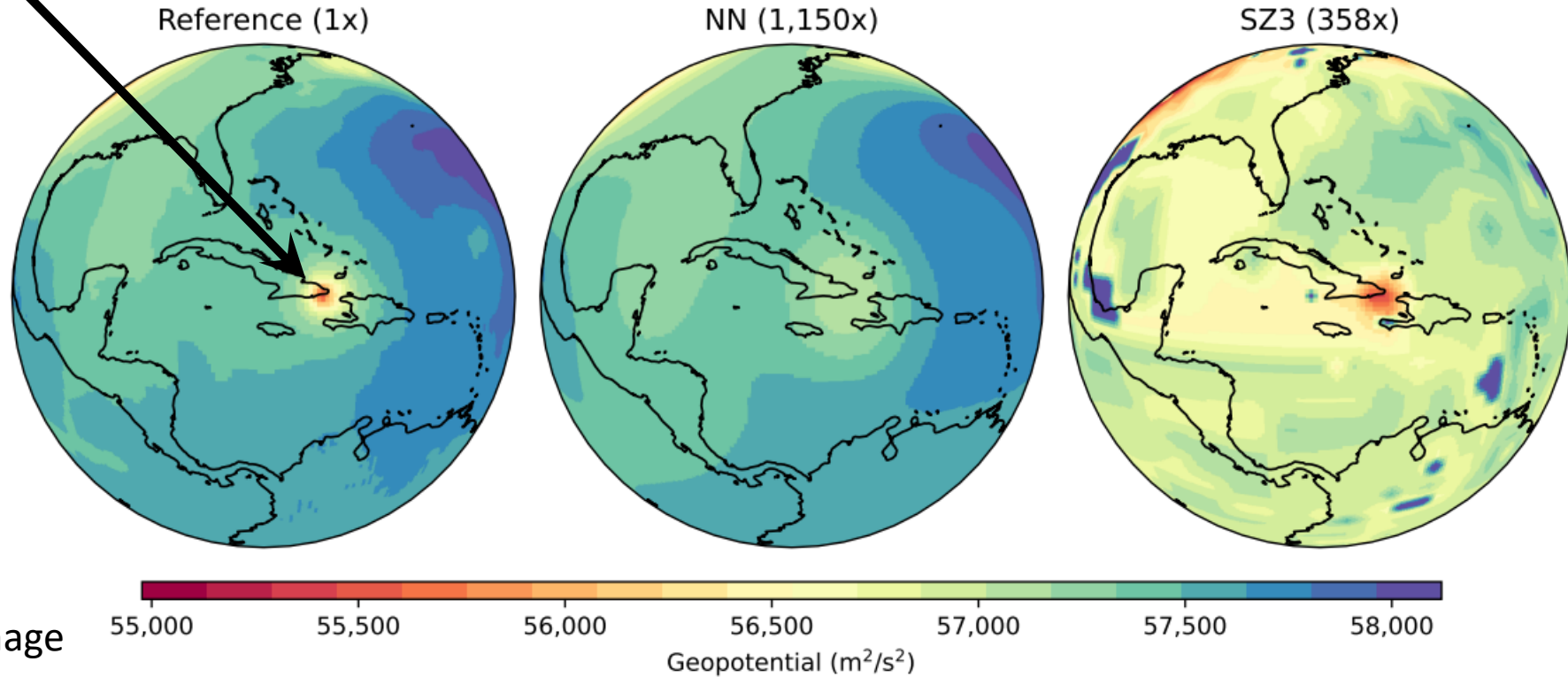
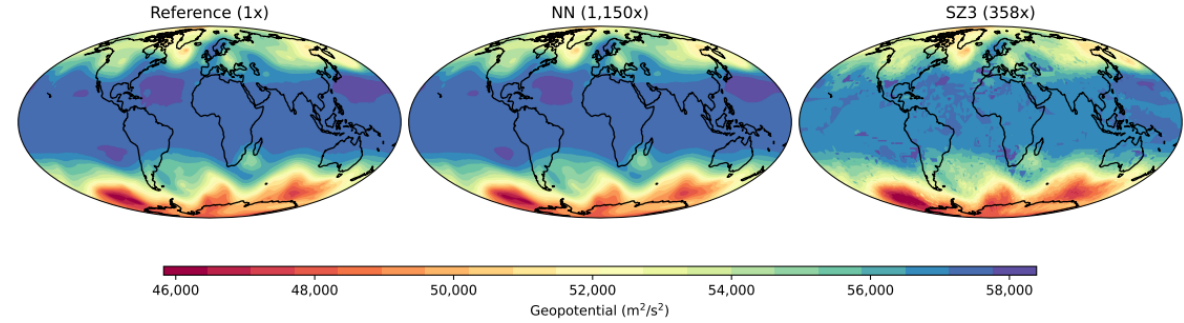
... and introduces artifacts:



Massive opportunity: Addressing the Climate Data Deluge (arXiv:2210.12538)

... but extreme events are dampened.

Hurricane Matthew (Oct. 5, 2016)



hit Cuba, Haiti, USA,
603 fatalities, \$16.5bn damage

[1]: Huang, Hoefler: "Compressing multidimensional weather and climate data into neural networks", ICLR'23 **top-5% paper**

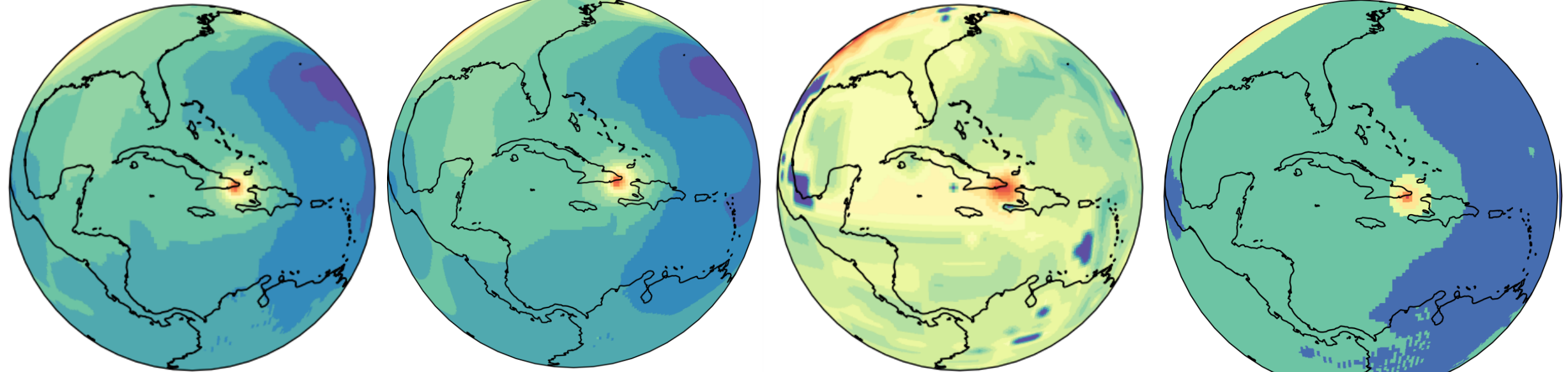
Meet the new wavelet basis – latest results from yesterday 😊

Reference (1x)

JP2Wavelet (1,115x)

SZ3 (358x)

rounding=0.7 CR=16



55,000 55,500 56,000 56,500 57,000 57,500 58,000
Geopotential (m^2/s^2)

Compressing atmospheric data into its real information content

[Milan Klöwer](#) , [Miha Razinger](#), [Juan J. Dominguez](#), [Peter D. Düben](#) & [Tim N. Palmer](#)

[Nature Computational Science](#) **1**, 713–724 (2021) | [Cite this article](#)

Summary

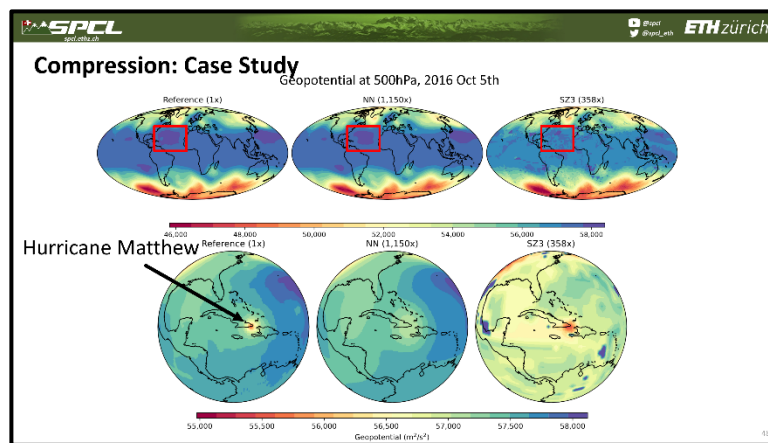
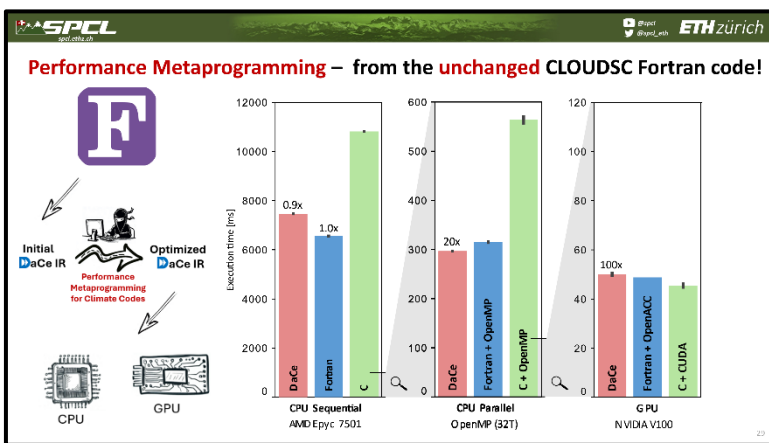
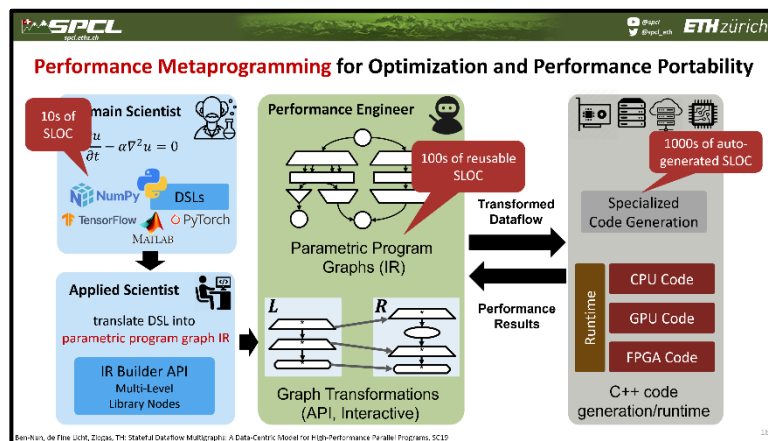
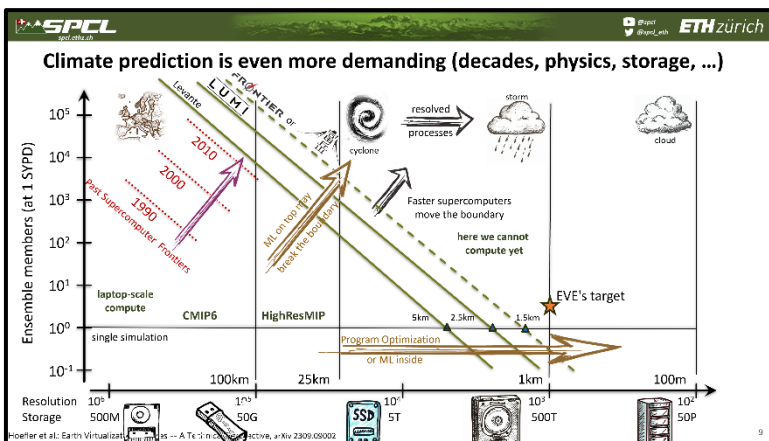
More of SPCL's research:

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twitter.com/spcl_eth **1.2K+ Followers**

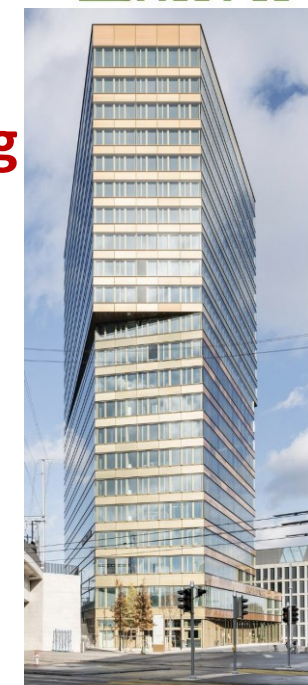
github.com/spcl **2K+ Stars**

... or spcl.ethz.ch



Join us! We're looking for PhD students, postdocs, and academic visitors in Zurich!

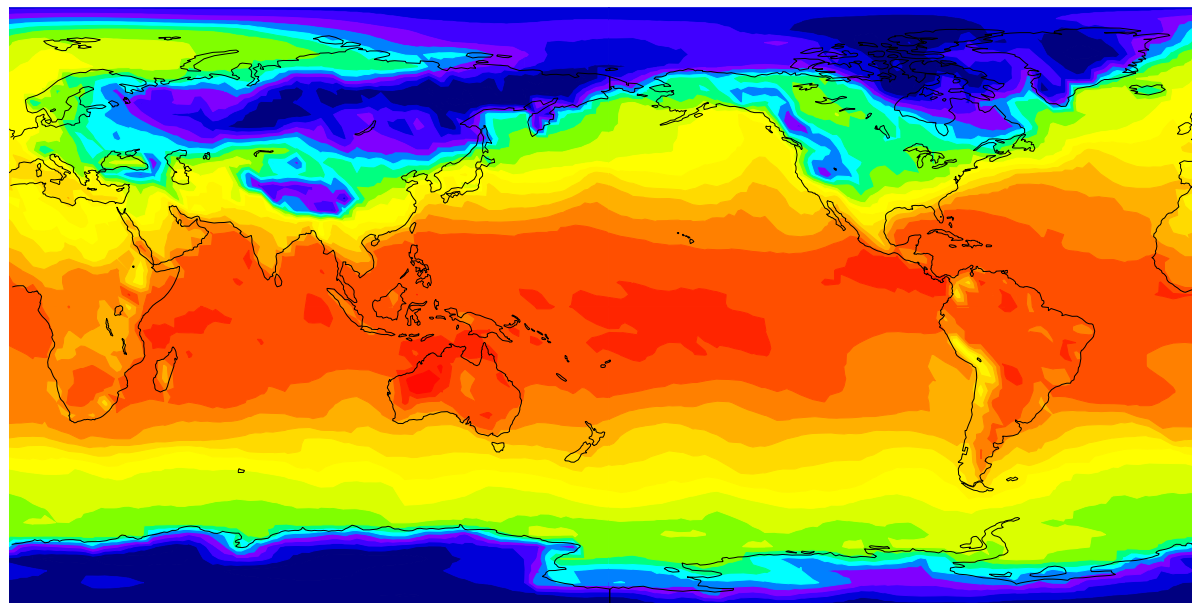
<http://spcl.inf.ethz.ch/Jobs/>



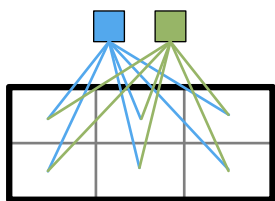
Bonus: Data Has Spatial Structure – Spatial Mixture of Experts

Weather and Climate grids have spatial structure!

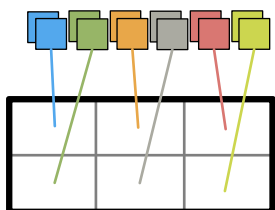
Locality matters!



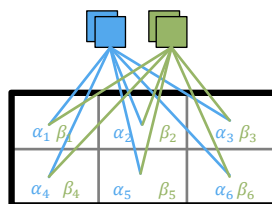
Convolution



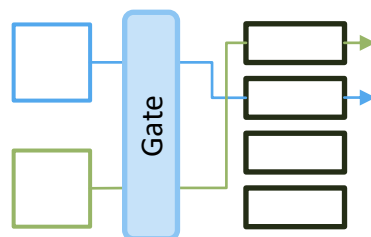
Locally-connected



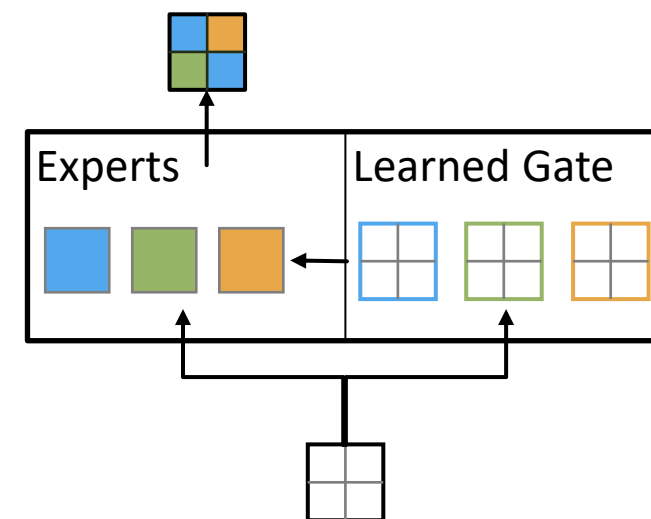
Low-rank locally-connected



Mixture-of-Experts

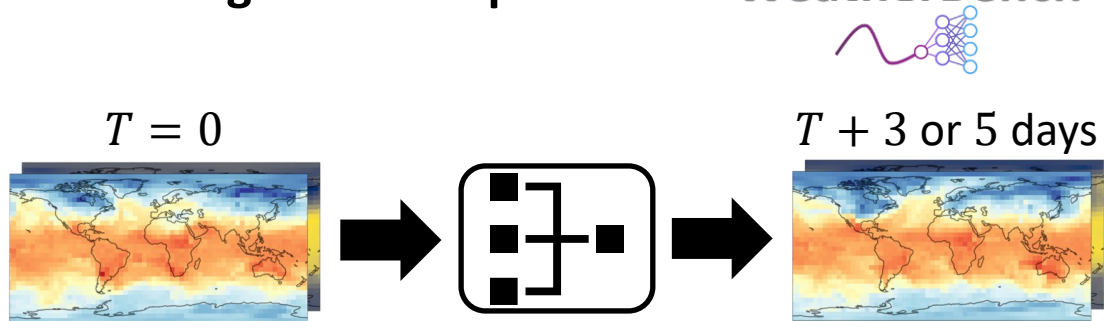


Spatial Mixture-of-Experts



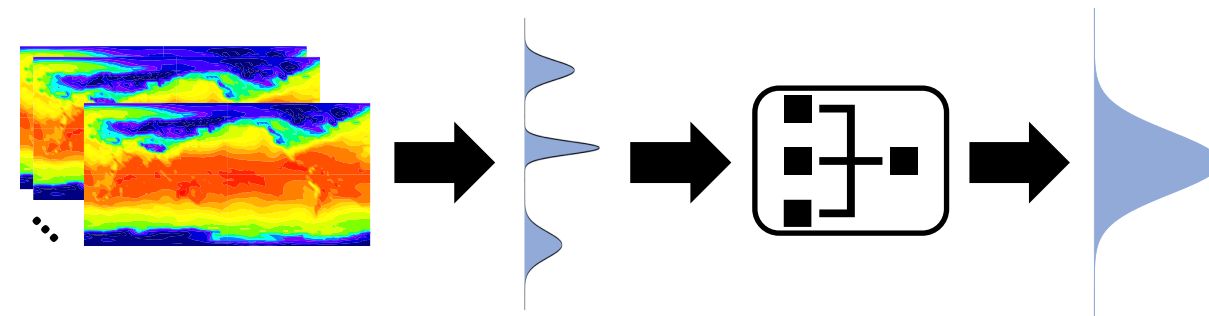
Spatial Mixture of Experts for Weather Prediction

Medium-range weather prediction 



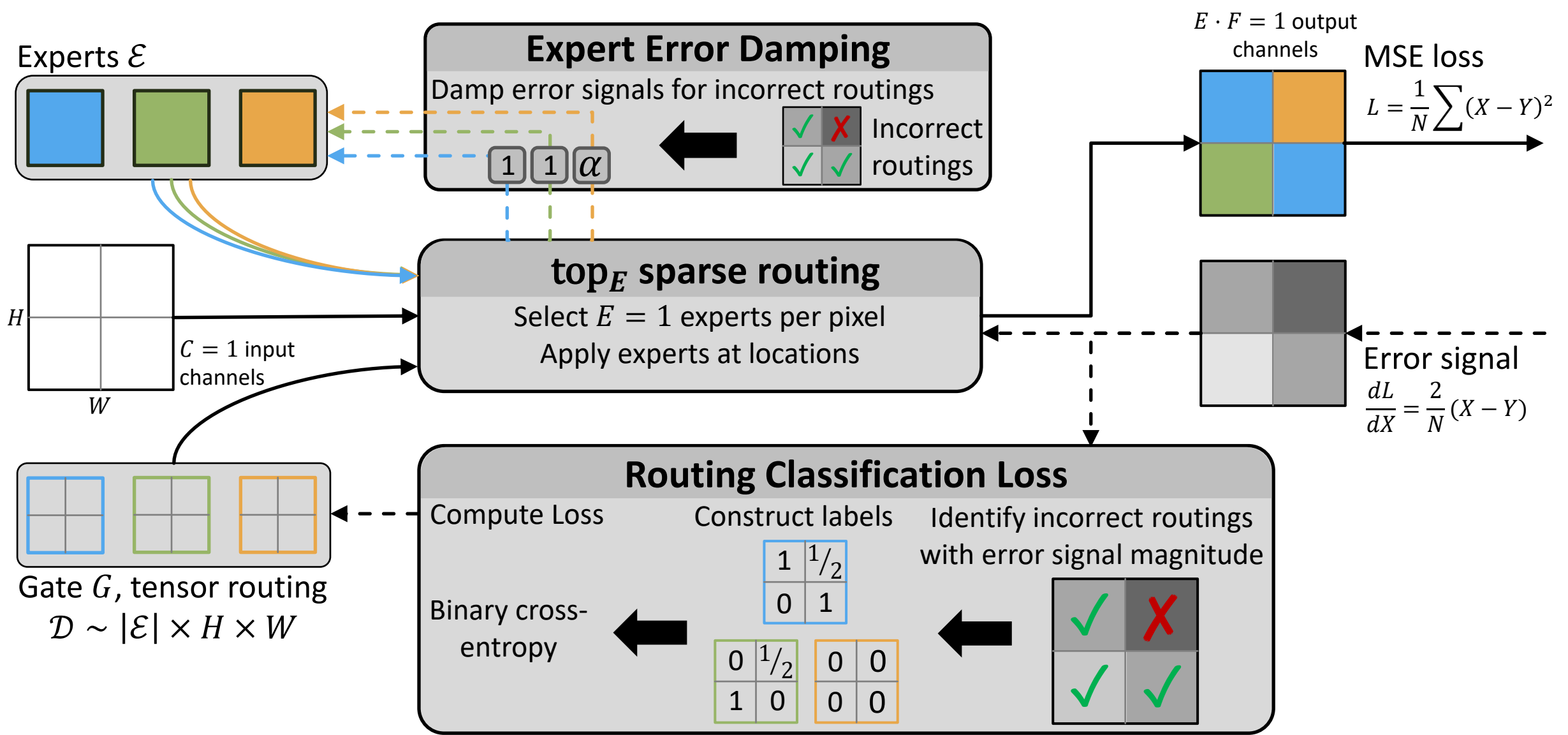
Model	Z500 [m^2s^{-2}]		T850 [K]	
	3 days	5 days	3 days	5 days
Rasp & Thurey	316 \pm 2.4	563 \pm 3.1	1.80 \pm 0.02	2.84 \pm 0.03
→ 2x wide	310 \pm 2.0	555 \pm 2.8	1.76 \pm 0.03	2.78 \pm 0.01
LRLCN	290 \pm 1.4	549 \pm 1.9	1.73 \pm 0.03	2.79 \pm 0.01
ViT	438 \pm 2.8	638 \pm 3.1	2.24 \pm 0.04	2.88 \pm 0.03
SMoE	270\pm2.0	525\pm2.0	1.66\pm0.02	2.60\pm0.01

Ensemble post-processing 



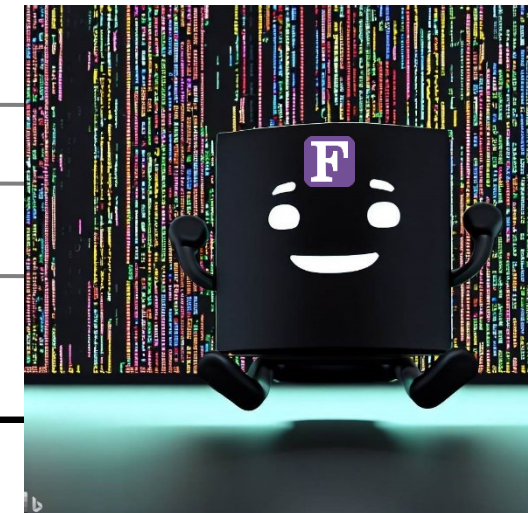
Model	Z500 [m^2s^{-2}]		T850 [K]		T2M [K]	
	5 ens	10 ens	5 ens	10 ens	5 ens	10 ens
CRPS						
EMOS	79.12 \pm 0.12	78.80 \pm 0.21	0.721 \pm 0.01	0.706 \pm 0.04	0.720 \pm 0.00	0.711 \pm 0.03
U-Net	76.54 \pm 0.20	76.18 \pm 0.12	0.685 \pm 0.00	0.670 \pm 0.01	0.657 \pm 0.01	0.644 \pm 0.01
SMoE	68.94\pm0.14	67.43\pm0.12	0.612\pm0.01	0.590\pm0.02	0.601\pm0.02	0.594\pm0.02
EECRPS						
EMOS	29.21 \pm 0.18	29.02 \pm 0.13	0.247 \pm 0.00	0.245 \pm 0.02	0.244 \pm 0.00	0.241 \pm 0.02
U-Net	27.78 \pm 0.11	27.55 \pm 0.19	0.230 \pm 0.01	0.229 \pm 0.01	0.225 \pm 0.00	0.220 \pm 0.01
SMoE	23.79\pm0.20	23.10\pm0.16	0.207\pm0.03	0.197\pm0.03	0.199\pm0.01	0.190\pm0.02

Spatial Mixture-of-Experts



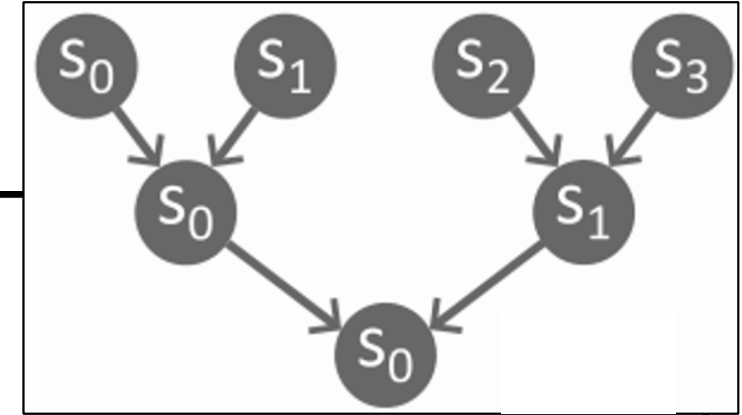
A first simple loop from CLOUDSC*

Data Parallelism	<pre> do JK=1, KLEV do JL=1, KFDIA ZQSM(JL, JK) = ZQSM(JL, JK) / (1.0 - RE * ZQSM(JL, JK)) enddo enddo </pre> <p style="color: green; text-align: right;">Fully data parallel</p>
Work	KLEV * KFDIA
Depth	1
Average Parallelism	KLEV * KFDIA

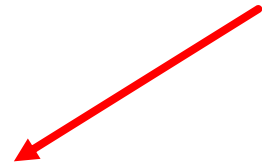


* examples are simplified for presentation purposes

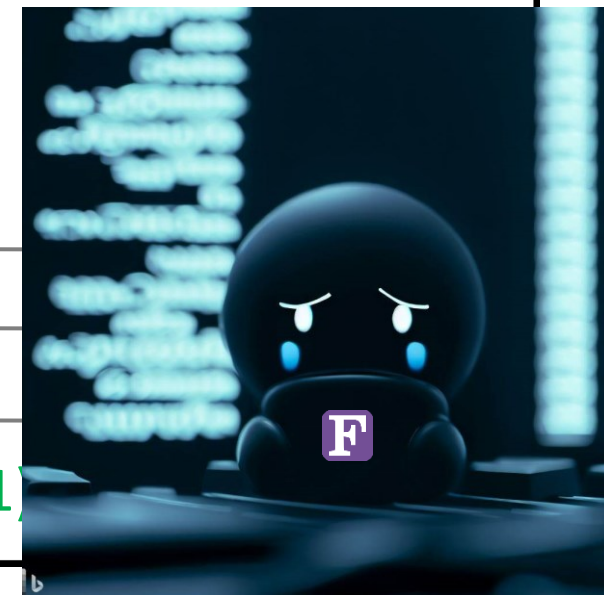
A second more complex loop from CLOUDSC



(array) accumulation prevents parallelization ☹️



Data Parallelism	<p>X do JN=1, NSTEP-1</p> <p>✓ do JL=1, KFDIA</p> <p style="text-align: center;">ZQXN(JL, NSTEP) = ZQXN(JL, NSTEP)+ZQXN(JL, JN)</p> <p> enddo</p> <p> enddo</p>
Work	<p>(NSTEP-1) * KFDIA (NSTEP-1) * KFDIA</p>
Depth	<p>(NSTEP-1) * KFDIA log₂(NSTEP-1)</p>
Average Parallelism	<p>1 (NSTEP-1) * KFDIA / log₂(NSTEP-1)</p>



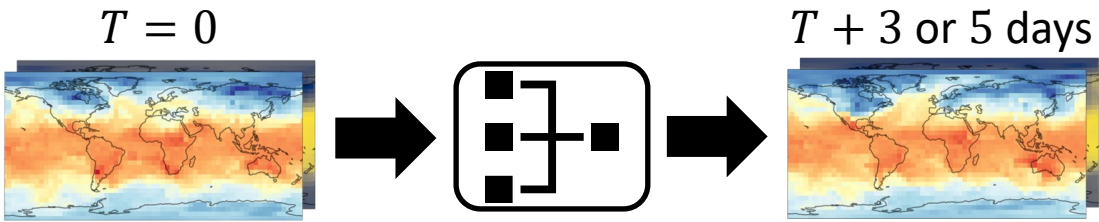
Now multiple realistic CLOUDSC loops

<p>Data Parallelism</p>				<p>Order Constraints</p> <p>Happens-before</p>				
<p>L1</p> <p>X do JM=1,4 X do JK=1,KLEV X do JL=1,KFDIA</p>	<pre> ① if ZQX(JL,JK, JM)<RLMIN) then ② ZQADJ=ZQX(JL, JK, JM)*ZQTMST ③ tend_q(JL, JK)=tend_q(JL, JK)+ZQADJ ④ tend_T(JL, JK)=tend_T(JL, JK) - RAL*Z ⑤ ZQX(JL, JK, JM)=0.0 </pre> <p style="color: red; text-align: center;">reuse of temporary variable prevents parallelization</p>			<p>① → ② Control ② → ③ RAW ② → ④ RAW ② → ⑤ WAR</p>				
<p>L2</p> <p>✓ do JK=1, KLEV ✓ do JL=1, KFDIA</p>	<pre> ⑥ ZQSM(JL, JK)=ZQSM(JL, JK)/(1.0-RE*ZQSM(JL, JK)) </pre>			<p>No order constraint</p> <p>② ①</p>				
<p>L3</p> <p>✓ do JK=1, KLEV ✓ do JL=1, KFDIA</p>	<pre> ⑦ ZA(JL, JK)=MAX(0.0, MIN(1.0, ZA(JL, JK))) ⑧ ZLI(JL, JK)=ZQX(JL, JK, 1)+ZQX(JL, JK, 2) ⑨ if (ZLI(JL, JK)>RLMIN) then ⑩ ZLFRAC(JL, JK)=ZQX(JL, JK, 1)/ZLI(JL, JK) else ⑪ ZLFRAC(JL, JK)=0.0 </pre>			<p>⑤ → ⑧ RAW ⑧ → ⑨ RAW ⑨ → ⑩ Control ⑨ → ⑪ Control</p> <p>③ → ①</p>				
<p>Work</p>	<p>L1</p>	<p>4 * KLEV * KFDIA * (1+4)</p>	<p>L2</p>	<p>KLEV * KFDIA</p>	<p>L3</p>	<p>KLEV * KFDIA * 4</p>	<p>L1</p>	<p>KLEV * KFDIA * 25</p>
<p>Depth</p>	<p>L1</p>	<p>log2(4) * 1 * 1 * (1+2)</p>	<p>L2</p>	<p>1</p>	<p>L3</p>	<p>1 * 1 * (2+1)</p>	<p>L2</p>	<p>8</p>
<p>Average Parallelism</p>	<p>L1</p>	<p>KLEV * KFDIA * 10/3</p>	<p>L2</p>	<p>KLEV * KFDIA</p>	<p>L3</p>	<p>KLEV * KFDIA * 4/3</p>	<p>L3</p>	<p>KLEV * KFDIA * 25/8</p>



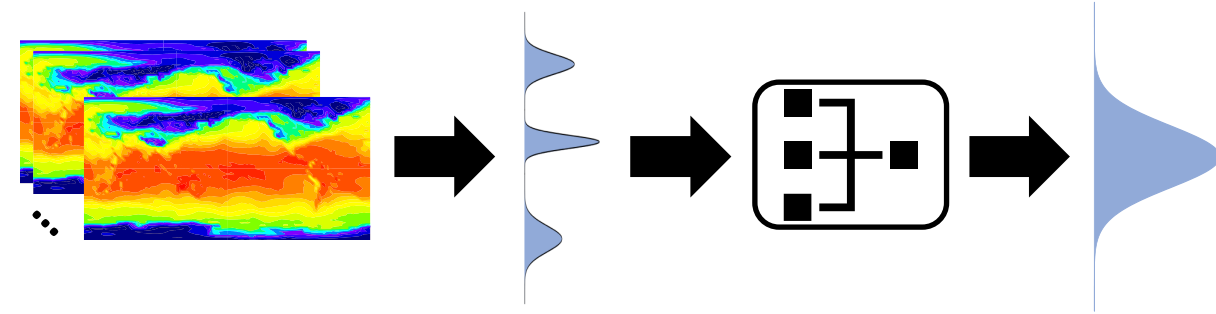
Weather

Medium-range weather prediction



Model	Z500 [m^2s^{-2}]		T850 [K]	
	3 days	5 days	3 days	5 days
Rasp & Thuerey	316 \pm 2.4	563 \pm 3.1	1.80 \pm 0.02	2.84 \pm 0.03
→ 2x wide	310 \pm 2.0	555 \pm 2.8	1.76 \pm 0.03	2.78 \pm 0.01
LRLCN	290 \pm 1.4	549 \pm 1.9	1.73 \pm 0.03	2.79 \pm 0.01
ViT	438 \pm 2.8	638 \pm 3.1	2.24 \pm 0.04	2.88 \pm 0.03
SMoE	270\pm2.0	525\pm2.0	1.66\pm0.02	2.60\pm0.01

Ensemble post-processing ENS-10



Model	Z500 [m^2s^{-2}]		T850 [K]		T2M [K]	
	5 ens	10 ens	5 ens	10 ens	5 ens	10 ens
CRPS						
EMOS	79.12 \pm 0.12	78.80 \pm 0.21	0.721 \pm 0.01	0.706 \pm 0.04	0.720 \pm 0.00	0.711 \pm 0.03
U-Net	76.54 \pm 0.20	76.18 \pm 0.12	0.685 \pm 0.00	0.670 \pm 0.01	0.657 \pm 0.01	0.644 \pm 0.01
SMoE	68.94\pm0.14	67.43\pm0.12	0.612\pm0.01	0.590\pm0.02	0.601\pm0.02	0.594\pm0.02
EECRPS						
EMOS	29.21 \pm 0.18	29.02 \pm 0.13	0.247 \pm 0.00	0.245 \pm 0.02	0.244 \pm 0.00	0.241 \pm 0.02
U-Net	27.78 \pm 0.11	27.55 \pm 0.19	0.230 \pm 0.01	0.229 \pm 0.01	0.225 \pm 0.00	0.220 \pm 0.01
SMoE	23.79\pm0.20	23.10\pm0.16	0.207\pm0.03	0.197\pm0.03	0.199\pm0.01	0.190\pm0.02